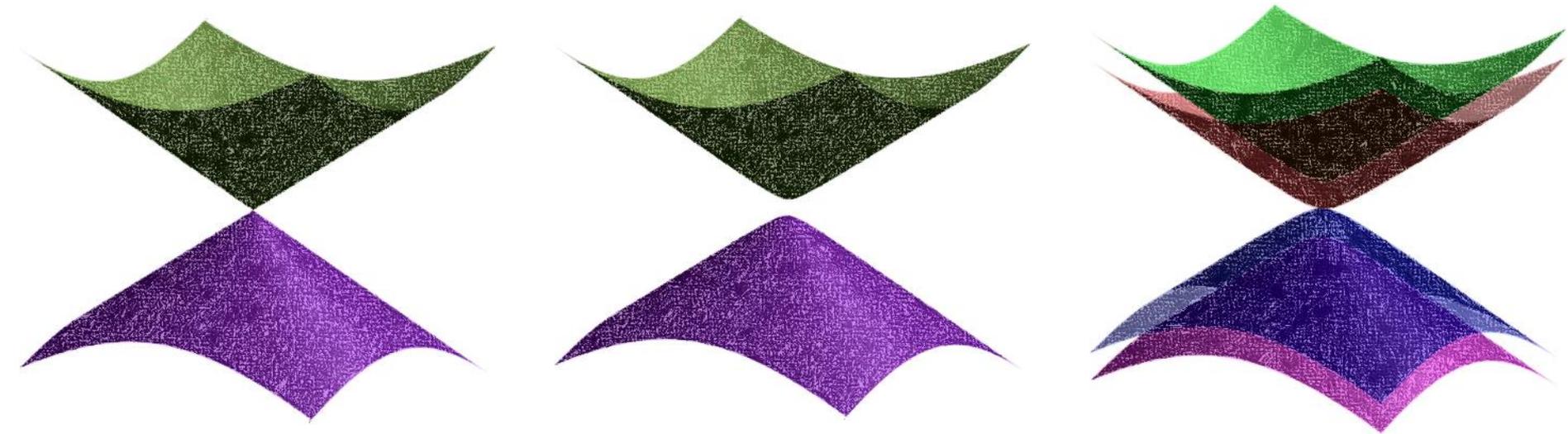


# 2D materials: An introduction



**Alessandro Cresti**

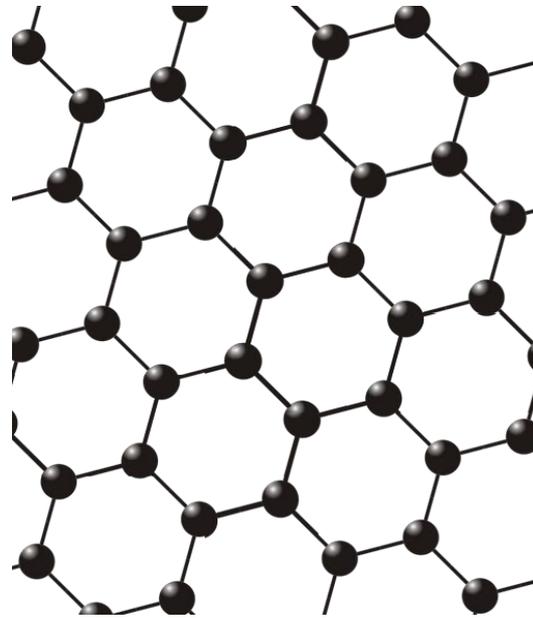
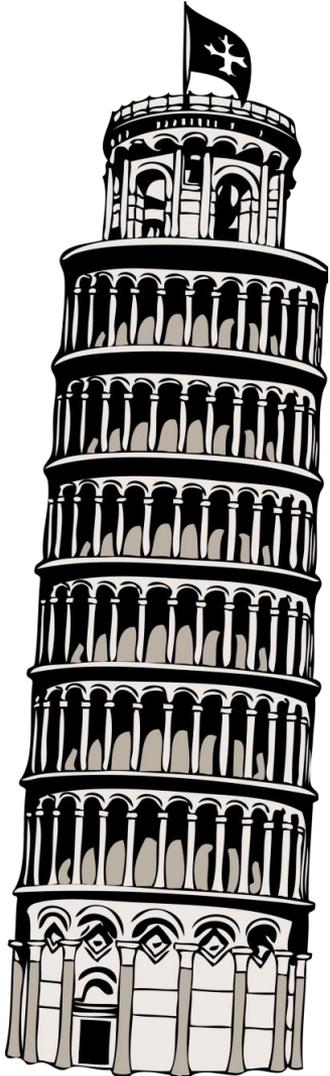
*alessandro.cresti@grenoble-inp.fr*

IMEP-LaHC / Grenoble INP / CNRS / Univ. Grenoble Alpes / Univ. Savoie Mont Blanc



# Some years ago in Pisa...

...I was a PhD student and my advisor told me...



**2005**

Band Structure and Optical Properties of Graphite and of the Layer Compounds GaS and GaSe (\*).

F. BASSANI (\*\*) and G. PASTORI PARRAVICINI (\*\*)

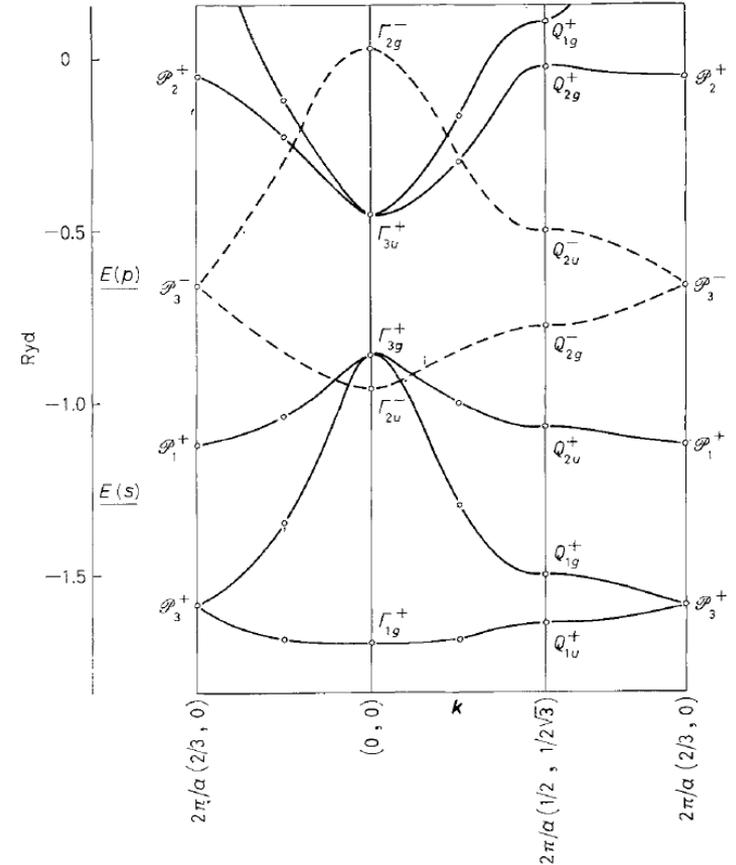


Fig. 5. - Band structure of two-dimensional graphite.

[Nuovo Cim. B 50, 95 (1967)]

**1967**

# Foreword: The discovery of graphene

PHYSICAL REVIEW

VOLUME 71, NUMBER 9

MAY 1, 1947

## The Band Theory of Graphite

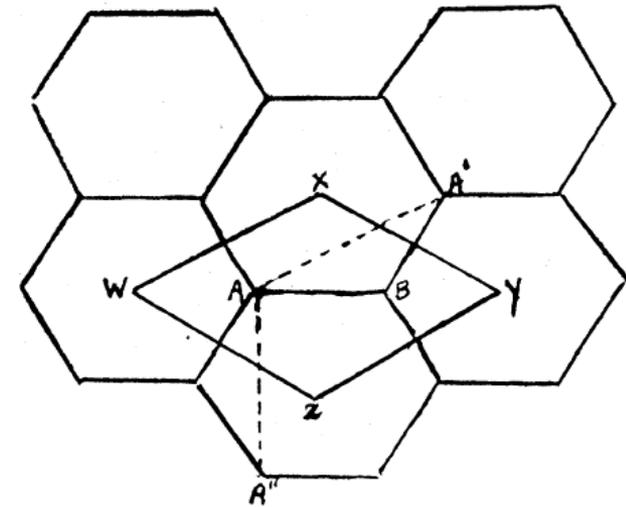
1947

P. R. WALLACE\*

*National Research Council of Canada, Chalk River Laboratory, Chalk River, Ontario*



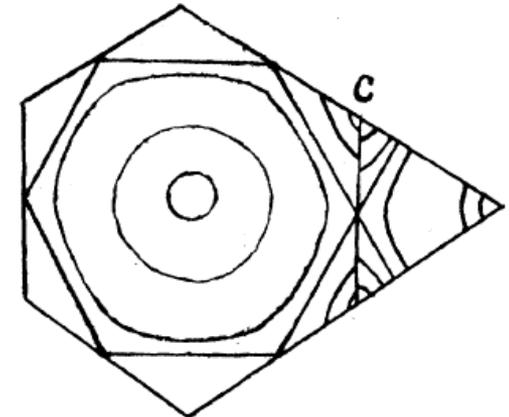
Philip R. Wallace



### 3. NUMBER OF FREE ELECTRONS AND CONDUCTIVITY OF A SINGLE HEXAGONAL LAYER

$$|E - E_c| \approx \sqrt{3}\pi\gamma_0 a |\mathbf{k} - \mathbf{k}_c|$$

*Linear mass-less relativistic dispersion*



# Foreword: The discovery of graphene

PHYSICAL REVIEW

VOLUME 104, NUMBER 3

NOVEMBER 1, 1956

## Diamagnetism of Graphite

J. W. McCLURE

**1956**

Using the abbreviation  $s = eH/\hbar c$ , we may then write

$$\kappa_n = [(2n+1)s]^{\frac{1}{2}}, \quad \epsilon_n = \pm \hbar v [(2n+1)s]^{\frac{1}{2}}. \quad (2.3)$$

***Relativistic Landau levels  
in graphene***

***Results for graphene were just a side product of those for graphite...  
graphene should not exist!***

Landau and Peierls predicted strictly 2D and infinitely extended materials to be unstable due to thermal fluctuations.

R. PEIERLS **1935**

Quelques propriétés typiques des corps solides

*Annales de l'I. H. P.*, tome 5, n° 3 (1935), p. 177-222

Indeed, real 2D materials have a finite size and may show 3D warping!

# Foreword: The discovery of graphene

## Electric Field Effect in Atomically Thin Carbon Films

K. S. Novoselov,<sup>1</sup> A. K. Geim,<sup>1\*</sup> S. V. Morozov,<sup>2</sup> D. Jiang,<sup>1</sup>  
Y. Zhang,<sup>1</sup> S. V. Dubonos,<sup>2</sup> I. V. Grigorieva,<sup>1</sup> A. A. Firsov<sup>2</sup>

22 OCTOBER 2004 VOL 306 SCIENCE

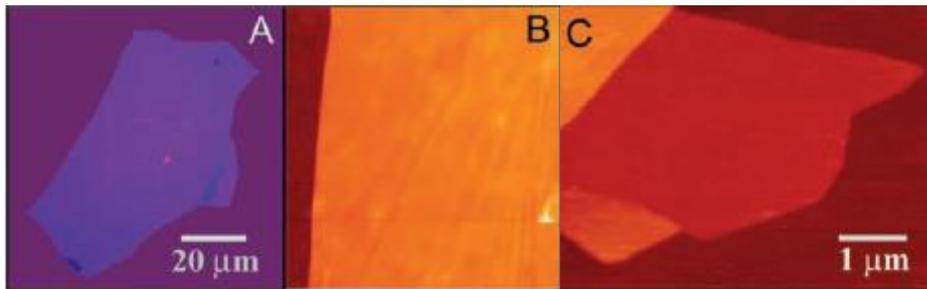
2004



A. Geim



K. Novoselov



2010 Nobel Prize

*“for groundbreaking experiments regarding the two-dimensional material graphene”*

# Foreword: The discovery of graphene

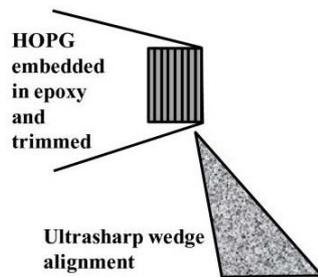


Ozyilmaz's Group, National University of Singapore - <https://www.youtube.com/watch?v=rphiCdR68TE>

# Foreword: The discovery of graphene

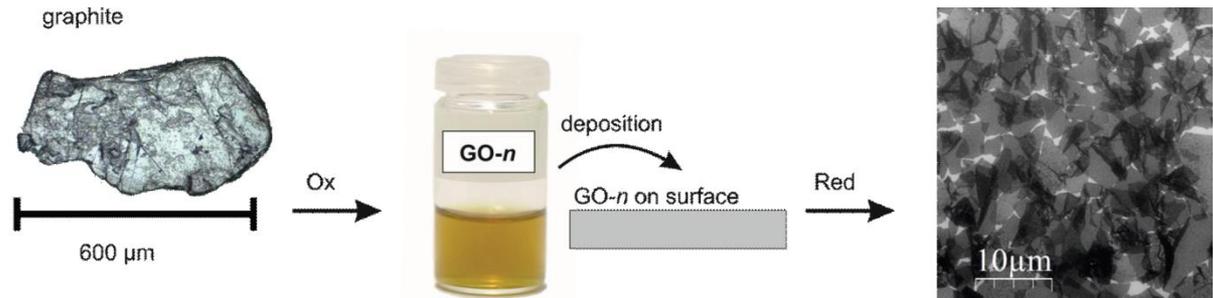
## Exfoliated graphene

### Mechanical cleavage



[Nanoscale Res. Lett. 6, 95 (2011)]

### Graphite oxide reduction



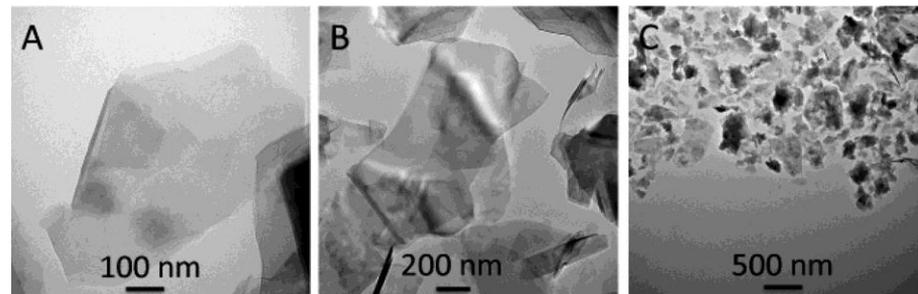
[S. Eigler et al., Adv. Mat. 25, 3583 (2013)]

### Shearing in liquid

[Nat. Mat. 13, 624 (2014)]



### Sonication

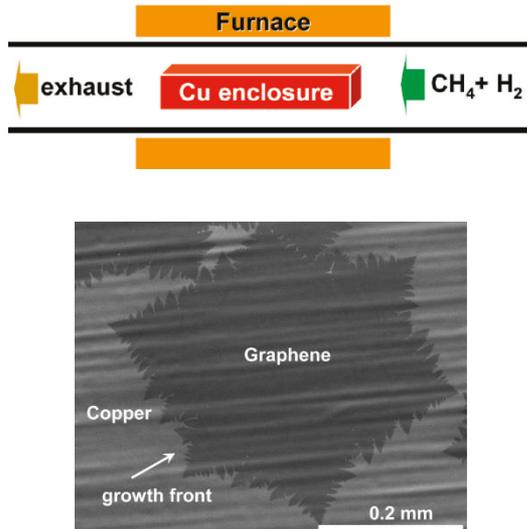


[S. J. Woltornist et al., ACS Nano 7, 7062 (2013)]

# Foreword: The discovery of graphene

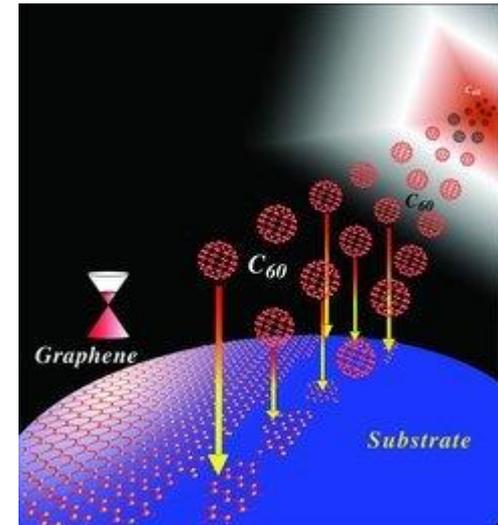
## Epitaxial graphene

### Chemical vapor deposition (CVD)



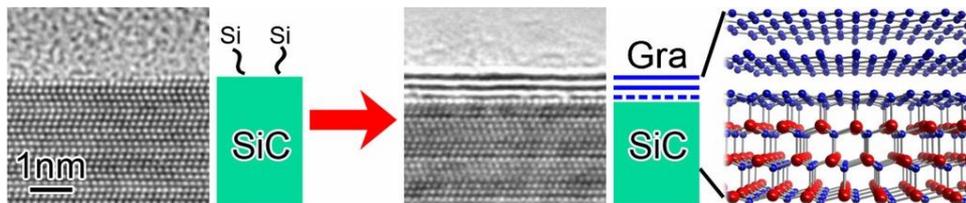
[X. Li et al., J. Am. Chem. Soc. 133, 2816 (2011)]

### Molecular beam epitaxy (MBE)

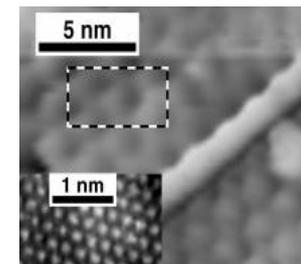


[J. Park et al., Adv. Mater. 22, 4140 (2010)]

### Thermal decomposition on the (0001) surface of 6H-SiC



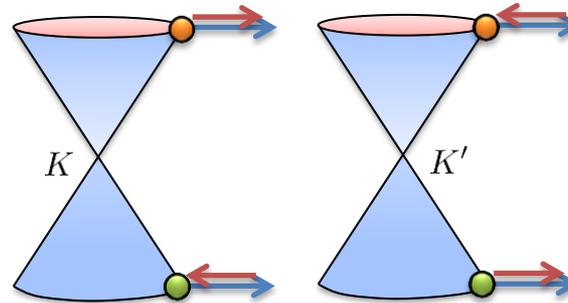
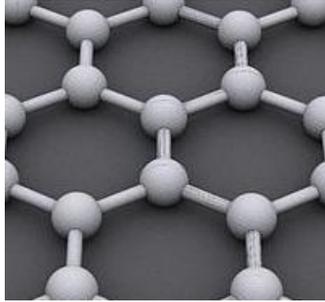
[W. Norimatsu et al., Semicond. Sci. Technol. 29, 064009 (2014)]



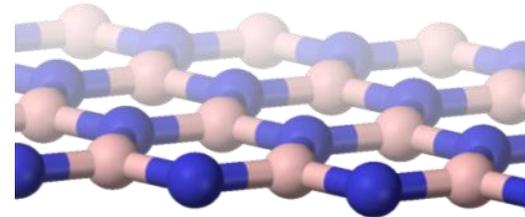
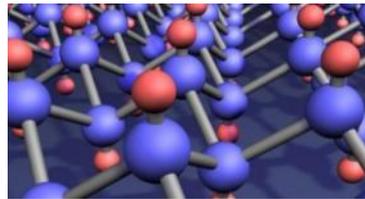
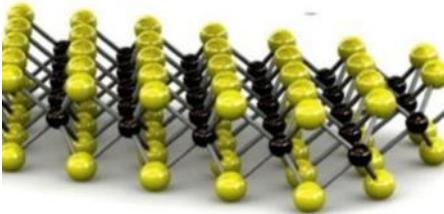
[C. Berger et al., J. Phys. Chem. B 108, 19913 (2004)]

# Plan

- Graphene: structure and properties



- Other 2D materials: TMDs, SMCs, X-enes, X-anes...

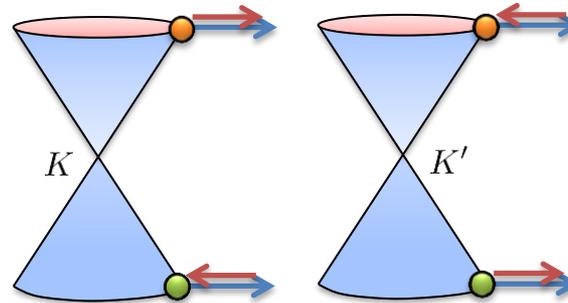
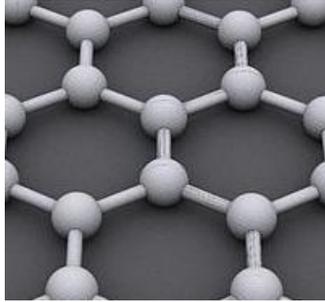


- Applications of 2D materials: electronics, optoelectronics, spintronics and many more

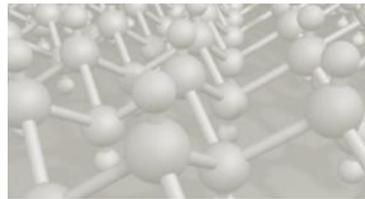
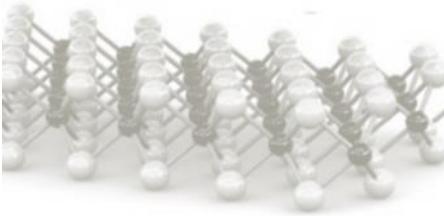


# Plan

- Graphene: structure and properties



- Other 2D materials: TMDs, SMCs, X-enes, X-anes...



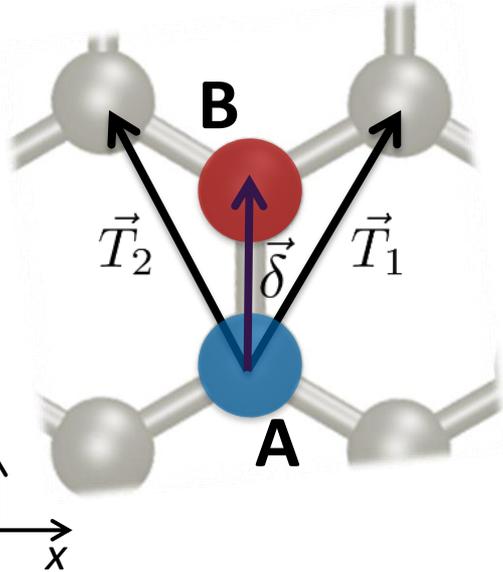
- Applications of 2D materials: electronics, optoelectronics, spintronics and many more



# Graphene lattice and reciprocal space

triangular lattice with basis (2 atoms per unit cell)

$$\vec{T}_1 = \begin{bmatrix} \frac{\sqrt{3}}{2}a \\ \frac{3}{2}a \end{bmatrix} \quad \vec{T}_2 = \begin{bmatrix} -\frac{\sqrt{3}}{2}a \\ \frac{3}{2}a \end{bmatrix} \quad \vec{\delta} = \begin{bmatrix} 0 \\ a \end{bmatrix}$$



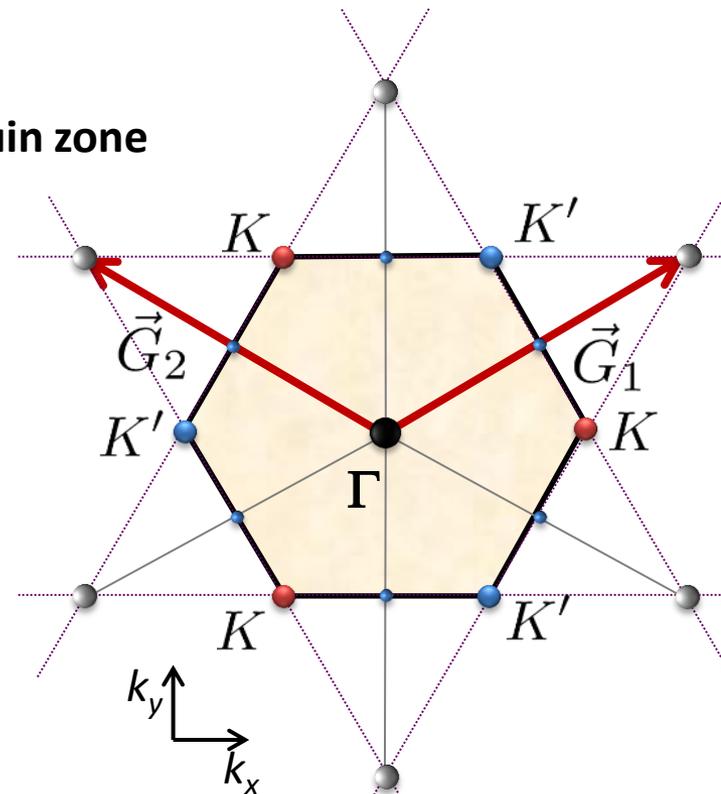
Reciprocal space

$$\vec{G}_i \cdot \vec{T}_j = 2\pi\delta_{ij}$$

$$\vec{G}_1 = \begin{bmatrix} \frac{2\pi}{\sqrt{3}a} \\ \frac{2\pi}{3a} \end{bmatrix} \quad \vec{G}_2 = \begin{bmatrix} -\frac{2\pi}{\sqrt{3}a} \\ \frac{2\pi}{3a} \end{bmatrix}$$

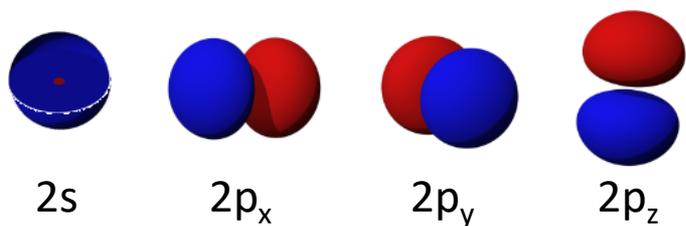
$$\Gamma = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \quad K = \begin{bmatrix} \frac{4\pi}{3\sqrt{3}a} \\ 0 \end{bmatrix} \quad K' = \begin{bmatrix} -\frac{4\pi}{3\sqrt{3}a} \\ 0 \end{bmatrix}$$

hexagonal Brillouin zone

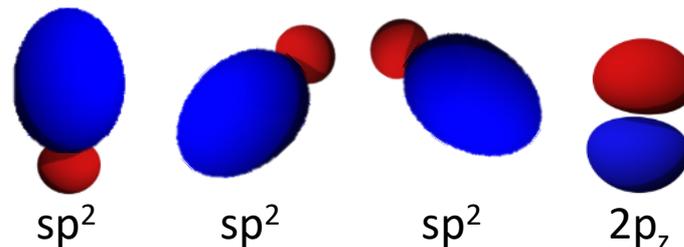


# A convenient orbital basis for graphene

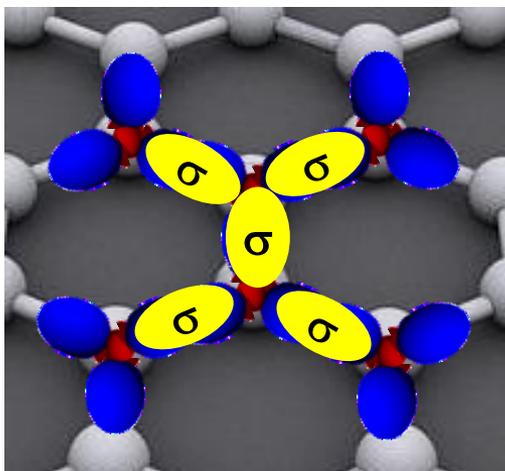
carbon electronic configuration [He]  $2s^2 2p^2$



$sp^2$  hybridization



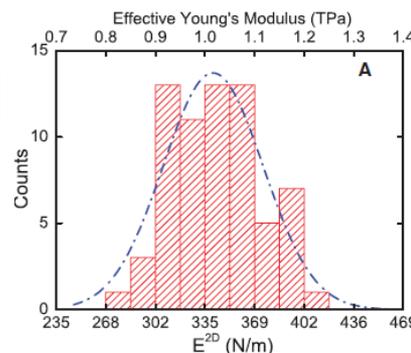
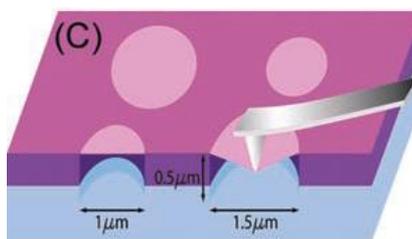
$\sigma$  bonds



Stiff  $\rightarrow$  Young's modulus  $1.0 \pm 0.1$  TPa

Strong  $\rightarrow$  tensile strength 130 GPa  $\rightarrow$  42 N/m

Stretchable  $\rightarrow$  up to 20%



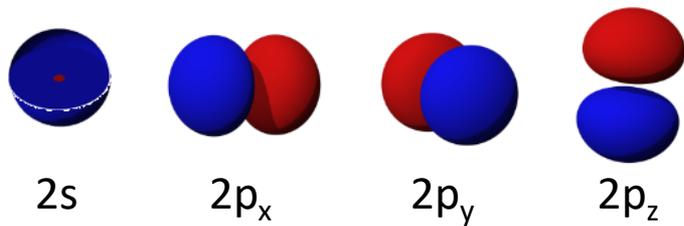
The  $sp^2$  orbitals form strong covalent  $\sigma$  bonds, which give mechanical stability to graphene and have high energy.



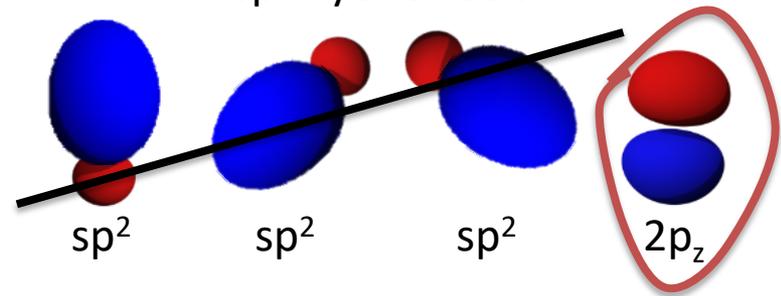
[D. G. Papageorgiou et al., Prog. Mat. Science 90, 75 (2017)]

# A convenient orbital basis for graphene

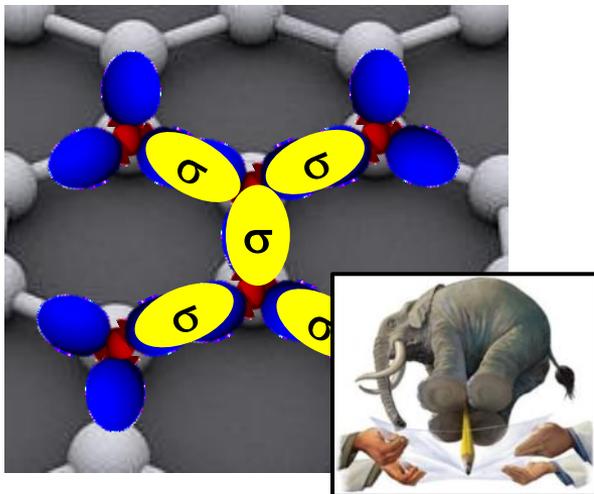
carbon electronic configuration [He]  $2s^2 2p^2$



$sp^2$  hybridization

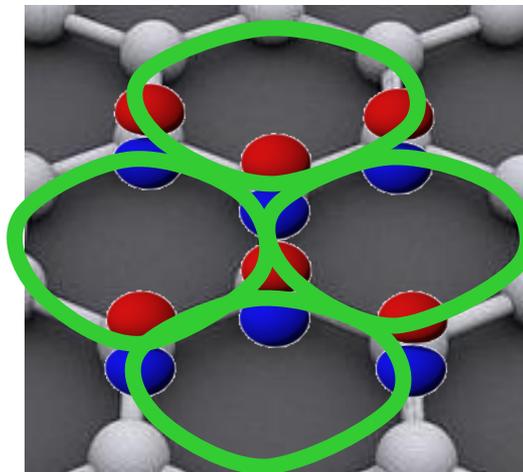


$\sigma$  bonds



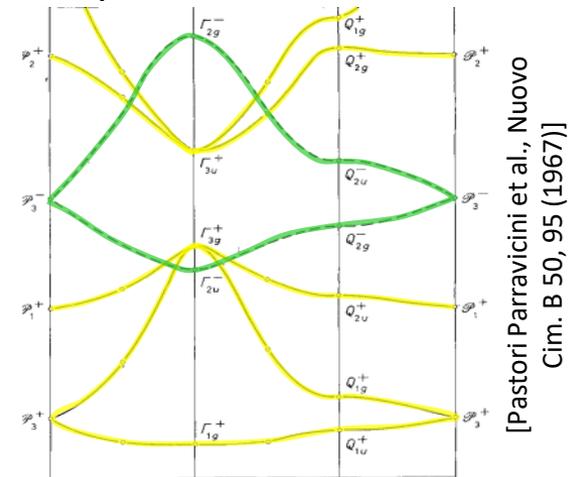
The  $sp^2$  orbitals form strong covalent  $\sigma$  bonds, which give mechanical stability to graphene and have high energy.

$\pi$  bonds



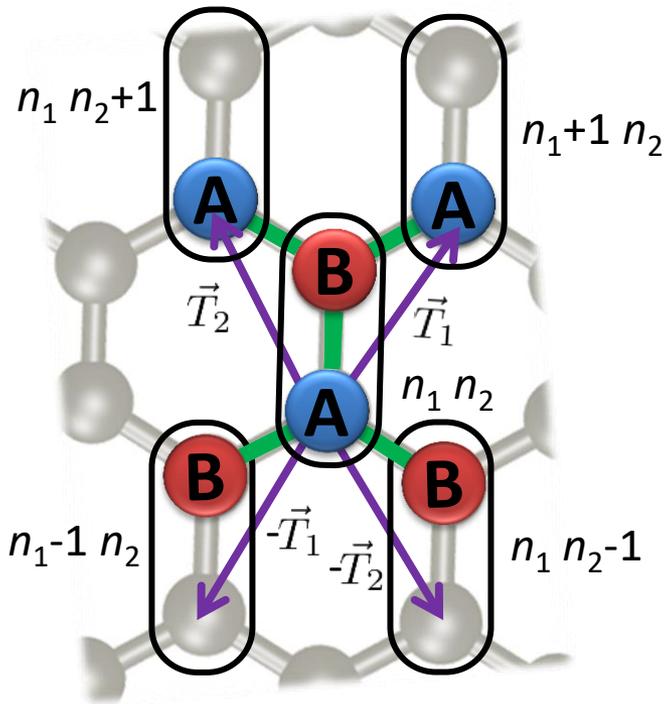
The  $2p_z$  orbitals form weaker and delocalized  $\pi$  bonds, which have low energy and determine the electronic properties.

complete band structure



For the description of the electron properties around the charge neutrality point, we can limit to  $2p_z$  orbitals.

# Graphene first-nearest-neighbor tight-binding Hamiltonian



## Bloch states

$$|\Phi^A(\vec{k})\rangle = \frac{1}{\sqrt{N}} \sum_{n_1 n_2} e^{i\vec{k} \cdot (n_1 \vec{T}_1 + n_2 \vec{T}_2)} |\phi_{n_1 n_2}^A\rangle$$

$$|\Phi^B(\vec{k})\rangle = \frac{1}{\sqrt{N}} \sum_{n_1 n_2} e^{i\vec{k} \cdot (n_1 \vec{T}_1 + n_2 \vec{T}_2)} |\phi_{n_1 n_2}^B\rangle$$

## Generic state with vector $k$

$$|\Psi(\vec{k})\rangle = \Psi^A(\vec{k})|\Phi^A(\vec{k})\rangle + \Psi^B(\vec{k})|\Phi^B(\vec{k})\rangle$$

basis :  $2p_z$  orbital per carbon atom



$$|\phi_{n_1 n_2}^A\rangle = |\phi_{2p_z}(n_1 \vec{T}_1 + n_2 \vec{T}_2)\rangle$$

$$|\phi_{n_1 n_2}^B\rangle = |\phi_{2p_z}(n_1 \vec{T}_1 + n_2 \vec{T}_2 + \vec{\delta})\rangle$$

## first-nearest-neighbor tight-binding Hamiltonian

$$H|\phi_{n_1 n_2}^A\rangle = t|\phi_{n_1 n_2}^B\rangle + t|\phi_{n_1-1, n_2}^B\rangle + t|\phi_{n_1, n_2-1}^B\rangle$$

$$H|\phi_{n_1 n_2}^B\rangle = t|\phi_{n_1 n_2}^A\rangle + t|\phi_{n_1+1, n_2}^A\rangle + t|\phi_{n_1, n_2+1}^A\rangle$$

## $k$ -dependent Hamiltonian

$$H|\Phi^A(\vec{k})\rangle = t \left( 1 + e^{-i\vec{k} \cdot \vec{T}_1} + e^{-i\vec{k} \cdot \vec{T}_2} \right) |\Phi^B(\vec{k})\rangle$$

$$H|\Phi^B(\vec{k})\rangle = t \left( 1 + e^{i\vec{k} \cdot \vec{T}_1} + e^{i\vec{k} \cdot \vec{T}_2} \right) |\Phi^A(\vec{k})\rangle$$

$$H(\vec{k}) = t \begin{bmatrix} 0 & f(\vec{k}) \\ f^*(\vec{k}) & 0 \end{bmatrix}$$

$$H(\vec{k}) \begin{bmatrix} \Psi^A(\vec{k}) \\ \Psi^B(\vec{k}) \end{bmatrix} = E(\vec{k}) \begin{bmatrix} \Psi^A(\vec{k}) \\ \Psi^B(\vec{k}) \end{bmatrix}$$

# Graphene energy bands

## $k$ -dependent Hamiltonian

$$H(\vec{k}) = t \begin{bmatrix} 0 & f(\vec{k}) \\ f^*(\vec{k}) & 0 \end{bmatrix} \quad f(\vec{k}) = 1 + 2e^{-i3ak_y/2} \cos(\sqrt{3}ak_x/2)$$

## Eigenvalues

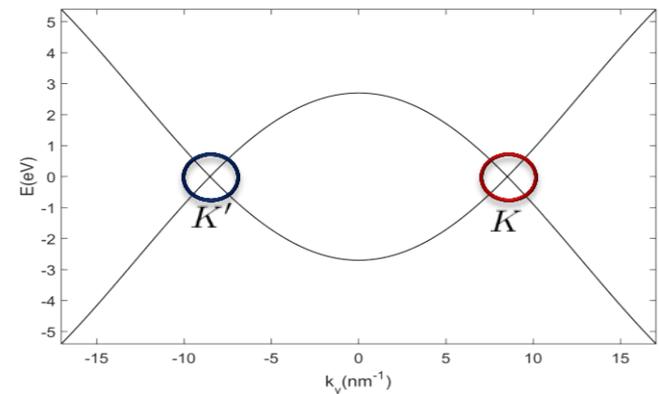
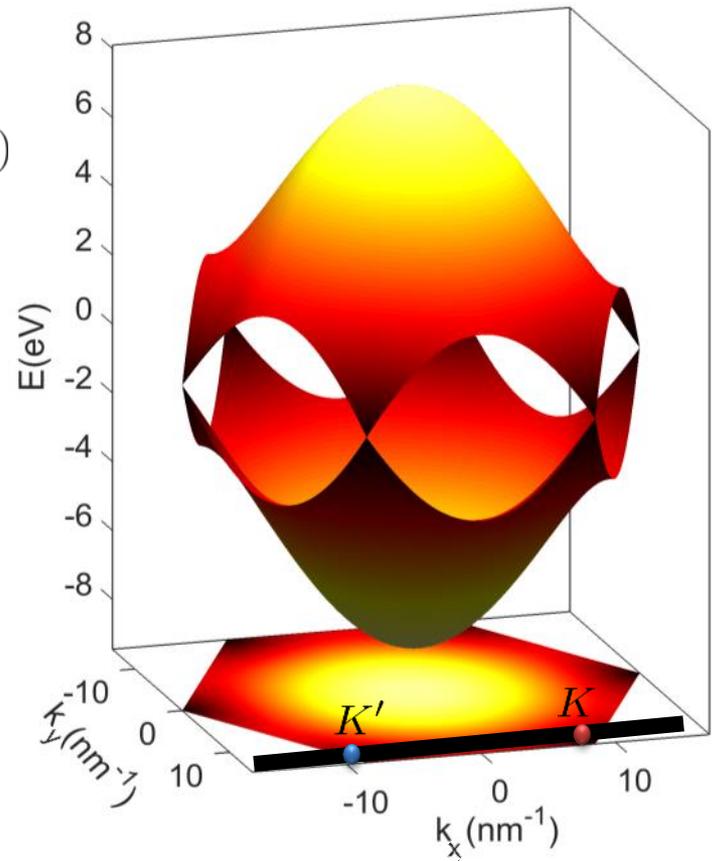
$$E(\vec{k}) = t\sqrt{1 + 4 \cos(3ak_y/2) \cos(\sqrt{3}ak_x/2) + 4 \cos^2(\sqrt{3}ak_x/2)}$$

## Eigenstates

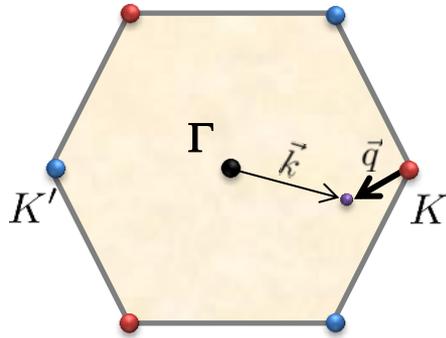
$$\begin{bmatrix} \Psi^A(\vec{k}) \\ \Psi^B(\vec{k}) \end{bmatrix}_{\pm} = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ \pm \frac{f(\vec{k})}{|f(\vec{k})|} \end{bmatrix}$$

$$|\Psi_{\pm}(\vec{k})\rangle = \frac{1}{\sqrt{2}}|\Phi^A(\vec{k})\rangle \pm \frac{1}{\sqrt{2}}\frac{f(\vec{k})}{|f(\vec{k})|}|\Phi^B(\vec{k})\rangle$$

- two components (A/B): **pseudospin**
- **semimetal** = zero band-gap semiconductor
- **linear isotropic dispersion (cones)** at K and K' points
- **low-energy** physics around K and K'



# Graphene – low energy approximation



For wave vectors close to the K point

$$\vec{k} = \vec{K} + \vec{q} = \left[ \frac{4\pi}{3\sqrt{3}a} + q_x ; q_y \right]$$

$$f(\vec{k}) = f(\vec{K} + \vec{q}) = 1 + 2e^{-i3aq_y/2} \cos(2\pi/3 + \sqrt{3}aq_x/2) \approx -\frac{3}{2}a(q_x - iq_y)$$

Pauli matrices operating on pseudospin

$$H_K(\vec{q}) \equiv H(\vec{K} + \vec{q}) \approx -\frac{3}{2}at \begin{bmatrix} 0 & q_x - iq_y \\ q_x + iq_y & 0 \end{bmatrix} = -\frac{3}{2}at \vec{\sigma} \cdot \vec{q}$$

2D Dirac equation for relativistic particles with spin 1/2

$$H_{2D}^{\text{Dirac}}(\vec{k}) = \hbar c \vec{\sigma} \cdot \vec{k} + mc^2 \sigma_z \quad E(\vec{k}) = \pm \sqrt{\hbar^2 c^2 k^2 + c^4 m^2}$$



Paul Dirac

• **spin** (Dirac equation)  $\leftrightarrow$  **pseudospin** (sublattice degree of freedom for graphene)

• **subluminal velocity**  $v = \frac{3a|t|}{2\hbar} \approx c/300$

• **zero mass**  $m = 0$

**K and K' = Dirac points**  
**linear energy dispersion = Dirac cones**

# Consequences of graphene band structure: charge mobility



The Fermi velocity is much larger than in other standard materials as silicon (~100 larger): **high charge mobility**

$$v_d = \mu E \rightarrow J = e(n \mu_e + p \mu_h) E$$

Labels for the equation:
 

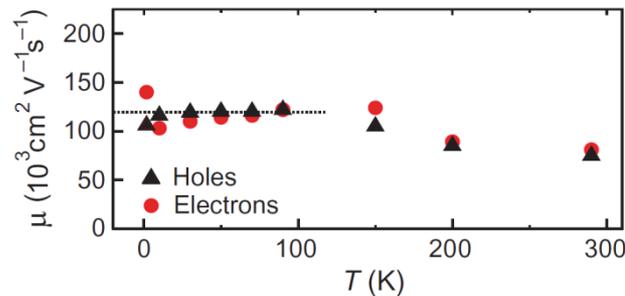
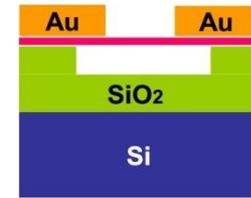
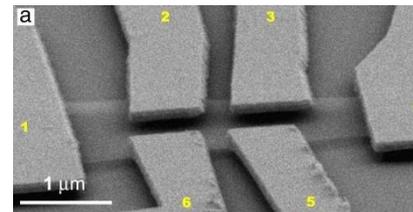
- electric field (points to  $E$ )
- current density (points to  $J$ )
- electron density (points to  $n$ )
- drift velocity (points to  $v_d$ )
- hole density (points to  $p$ )

Exfoliated graphene over SiO<sub>2</sub>  $\mu \leq 25\,000 \text{ cm}^2/(\text{Vs})$  @  $n = 5 \times 10^{12} \text{ cm}^{-2}$  [PRL 99, 246803 (2007)]

Suspended exfoliated graphene

$$\mu = 230\,000 \text{ cm}^2/(\text{Vs}) \text{ @ } n = 2 \times 10^{11} \text{ cm}^{-2}$$

[Sol. State Comm. 146, 351 (2008)]



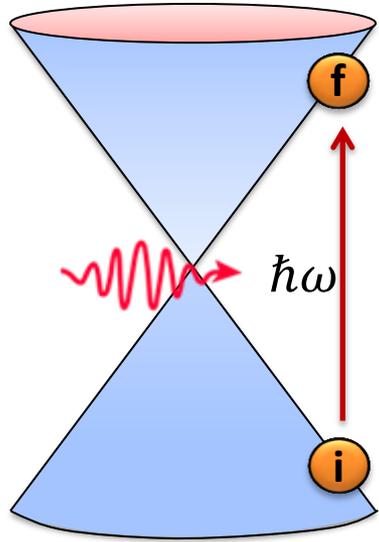
CVD graphene encapsulated in hBN

$$\mu > 100\,000 \text{ cm}^2/(\text{Vs})$$

[Science Adv. 1, e1500222 (2015)]

Crystalline silicon  $\mu \approx 1\,500 \text{ cm}^2/(\text{Vs})$  @300K - AlGaAs/GaAs 2DEGs  $\mu \approx 35\,000\,000 \text{ cm}^2/(\text{Vs})$

# Consequences of graphene band structure: optical absorption



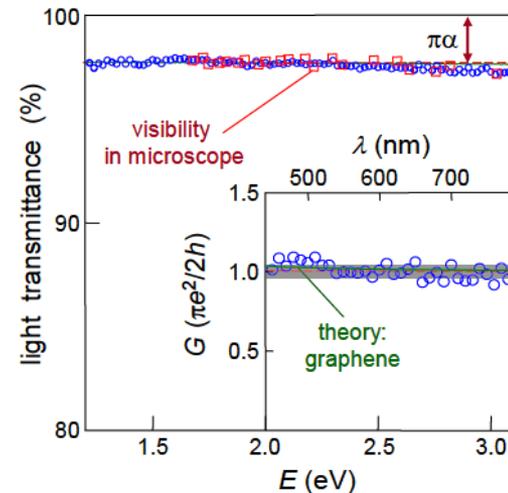
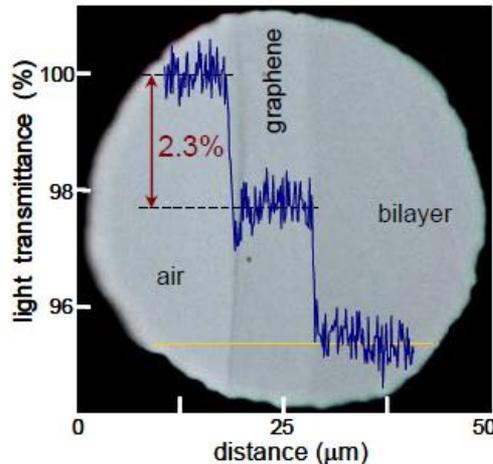
$$E = eE e^{i\omega t} \quad W_i = \frac{c}{4\pi} E^2 \quad W_a = \eta \hbar \omega \quad \eta = \frac{2\pi}{\hbar} |M|^2 \rho \left( \frac{\hbar\omega}{2} \right)$$

$$\rho \left( \frac{\hbar\omega}{2} \right) = \frac{\hbar\omega}{\pi \hbar^2 v_F^2} \quad H = v_F \boldsymbol{\sigma} \cdot \boldsymbol{\pi} = v_F \boldsymbol{\sigma} \cdot \left( \mathbf{p} - \frac{e}{c} \mathbf{A} \right) = H_0 + H_{\text{int}}$$

$$\mathbf{A} = \frac{i}{c\omega} \mathbf{E} \leftarrow \mathbf{E} = c \partial_t \mathbf{A} \quad H_{\text{int}} = -\frac{ev_F}{c} \boldsymbol{\sigma} \cdot \mathbf{A} = -i \frac{ev_F}{c\omega} E \boldsymbol{\sigma} \cdot \mathbf{e}$$

$$|M|^2 = \left| \left\langle f \left| \frac{ev_F}{i\omega} E \boldsymbol{\sigma} \cdot \mathbf{e} \right| i \right\rangle \right|^2 = \frac{e^2 v_F^2 E^2}{8\omega^2} \quad W_a = \frac{e^2}{4\hbar} E^2 \rightarrow \frac{W_a}{W_i} = \frac{\pi e^2}{\hbar c} = \pi \alpha$$

Constant optical absorption **~2.3%** over a wide spectrum



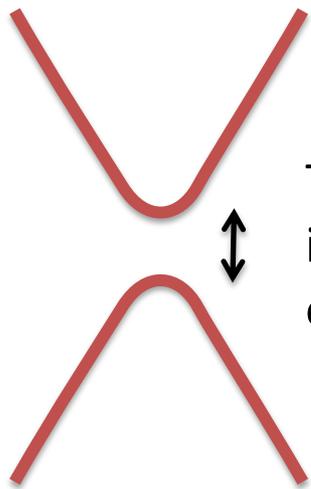
[R.R. Nair et al., Science 320, 1308 (2008)]

# Spin-orbit coupling in the graphene

A **moving magnetic dipole generates an electric dipole**, which interacts with the electric field.

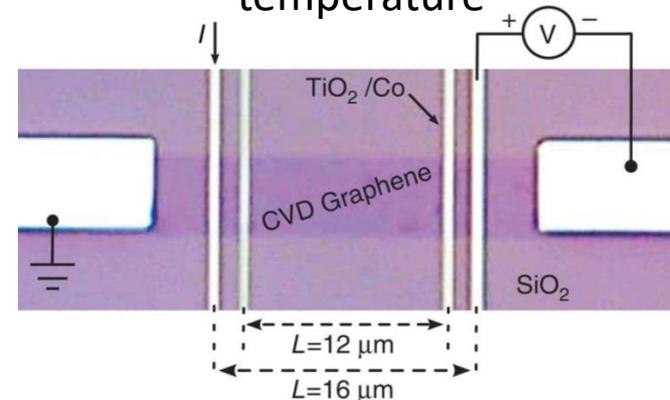
$$H_I = -\frac{e\hbar}{4m^2c^2} (\vec{\nabla}V \times \vec{p}) \cdot \vec{s} = \begin{cases} -\frac{e\hbar}{4m^2c^2} \frac{\partial_r V(r)}{r} \vec{L} \cdot \vec{s} & \text{intrinsic SOC} \\ \frac{e\hbar}{4m^2c^2} (\vec{p} \times \vec{s}) \cdot \vec{E} & \text{Rashba SOC} \end{cases}$$

As a consequence, **spin-orbit coupling couples  $\pi$ ,  $\sigma$  and higher energy bands**.



The resulting **spin-orbit gap** in graphene is in the order of  **$20\mu\text{eV}$** , i.e. **very small!**

Spin transmission **over  $16\mu\text{m}$**  at room temperature

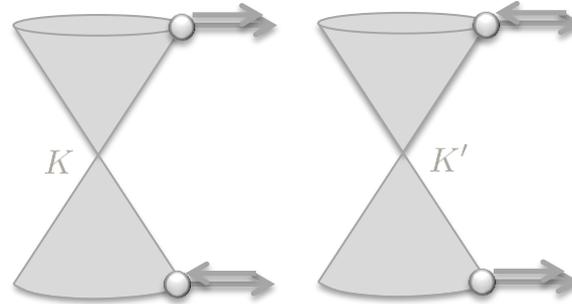
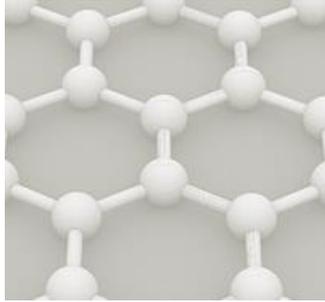


[M. V. Kamalakar et al., Nat. Comm. 6, 6766 (2015)]

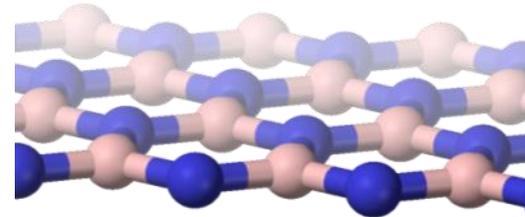
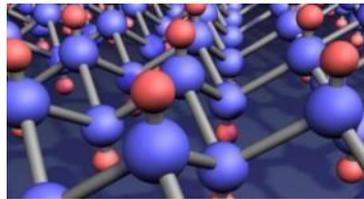
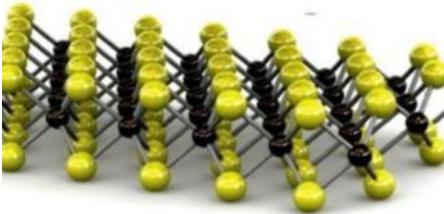
 [H. Min et al., PRB 74, 165310 (2006); S. Konschuh et al., PRB 82, 245412 (2010)]

# Plan

- Graphene: structure and properties



- Other 2D materials: TMDs, SMCs, X-enes, X-anes...



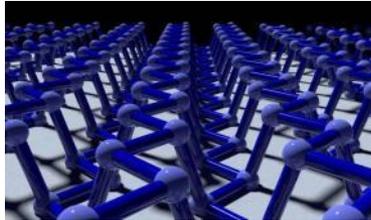
- Applications of 2D materials: electronics, optoelectronics, spintronics and many more



# Many 2D materials

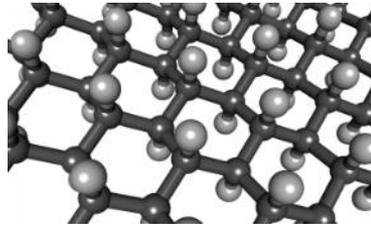
## X-enes

*graphene, silicene, germanene, phosphorene, stanene*



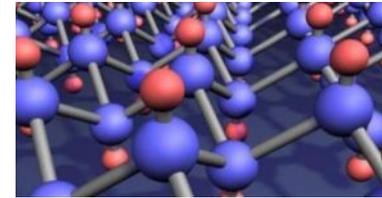
## X-anes

*graphane, silicane, germanane, phosphorane, stanane*

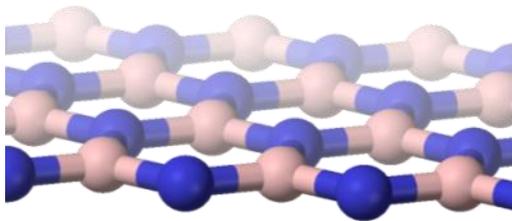


## Fluoro-X-enes

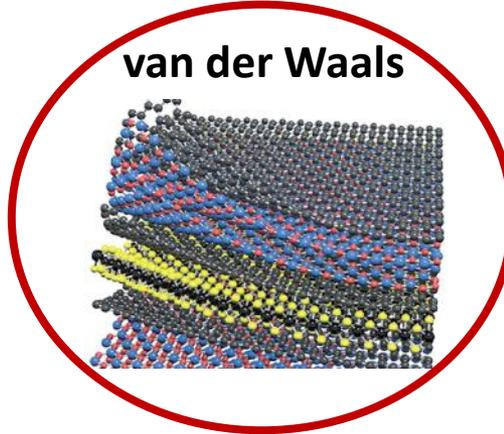
*fluorographene, fluorosilicene, fluorogermanene*



## hBN

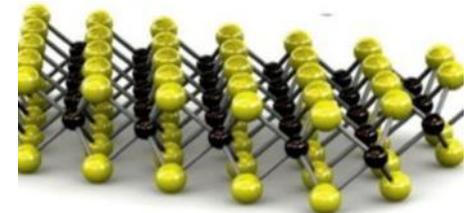


## van der Waals



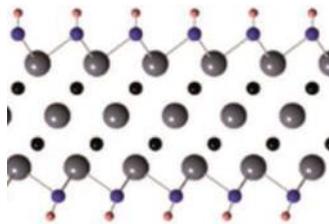
## TMDs

transition metal (group IV, V and V)  
+ 2 chalcogens (S, Se, Te)



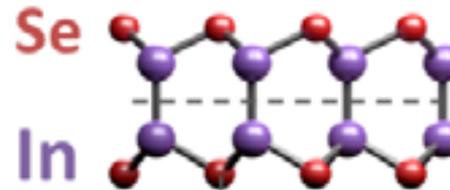
## MX-enes

transition metal + C/N



## SMCs

semimetal (Ga, In) + chalcogen (S, Se)



[P. Miró, M. Audiffred and T. Heine, *An atlas of two-dimensional materials*, Chem. Soc. Rev. 43, 6537 (2014)]

# X-enes group

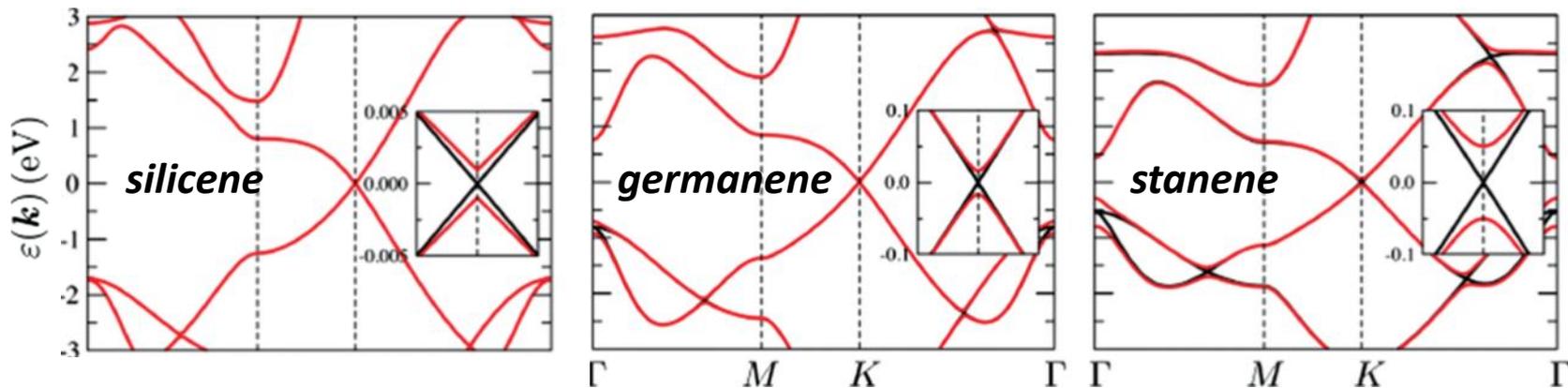
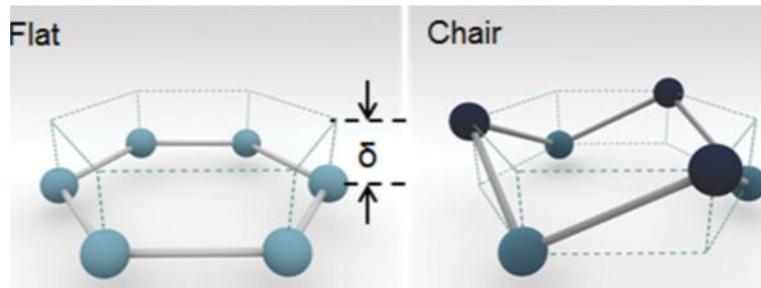
Single-layer **single-element materials** with hexagonal lattice.

| Group →     | 1        | 2        | 3        | 4         | 5         | 6         | 7         | 8         | 9         | 10        | 11        | 12        | 13        | 14        | 15        | 16        | 17        | 18        |
|-------------|----------|----------|----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| ↓ Period    |          |          |          |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |
| 1           | 1<br>H   |          |          |           |           |           |           |           |           |           |           |           |           |           |           |           |           | 2<br>He   |
| 2           | 3<br>Li  | 4<br>Be  |          |           |           |           |           |           |           |           |           |           | 5<br>B    | 6<br>C    | 7<br>N    | 8<br>O    | 9<br>F    | 10<br>Ne  |
| 3           | 11<br>Na | 12<br>Mg |          |           |           |           |           |           |           |           |           |           | 13<br>Al  | 14<br>Si  | 15<br>P   | 16<br>S   | 17<br>Cl  | 18<br>Ar  |
| 4           | 19<br>K  | 20<br>Ca | 21<br>Sc | 22<br>Ti  | 23<br>V   | 24<br>Cr  | 25<br>Mn  | 26<br>Fe  | 27<br>Co  | 28<br>Ni  | 29<br>Cu  | 30<br>Zn  | 31<br>Ga  | 32<br>Ge  | 33<br>As  | 34<br>Se  | 35<br>Br  | 36<br>Kr  |
| 5           | 37<br>Rb | 38<br>Sr | 39<br>Y  | 40<br>Zr  | 41<br>Nb  | 42<br>Mo  | 43<br>Tc  | 44<br>Ru  | 45<br>Rh  | 46<br>Pd  | 47<br>Ag  | 48<br>Cd  | 49<br>In  | 50<br>Sn  | 51<br>Sb  | 52<br>Te  | 53<br>I   | 54<br>Xe  |
| 6           | 55<br>Cs | 56<br>Ba |          | 72<br>Hf  | 73<br>Ta  | 74<br>W   | 75<br>Re  | 76<br>Os  | 77<br>Ir  | 78<br>Pt  | 79<br>Au  | 80<br>Hg  | 81<br>Tl  | 82<br>Pb  | 83<br>Bi  | 84<br>Po  | 85<br>At  | 86<br>Rn  |
| 7           | 87<br>Fr | 88<br>Ra |          | 104<br>Rf | 105<br>Db | 106<br>Sg | 107<br>Bh | 108<br>Hs | 109<br>Mt | 110<br>Ds | 111<br>Rg | 112<br>Cn | 113<br>Nh | 114<br>Fl | 115<br>Mc | 116<br>Lv | 117<br>Ts | 118<br>Og |
| Lanthanides |          |          |          |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |
|             | 57<br>La | 58<br>Ce | 59<br>Pr | 60<br>Nd  | 61<br>Pm  | 62<br>Sm  | 63<br>Eu  | 64<br>Gd  | 65<br>Tb  | 66<br>Dy  | 67<br>Ho  | 68<br>Er  | 69<br>Tm  | 70<br>Yb  | 71<br>Lu  |           |           |           |
| Actinides   |          |          |          |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |
|             | 89<br>Ac | 90<br>Th | 91<br>Pa | 92<br>U   | 93<br>Np  | 94<br>Pu  | 95<br>Am  | 96<br>Cm  | 97<br>Bk  | 98<br>Cf  | 99<br>Es  | 100<br>Fm | 101<br>Md | 102<br>No | 103<br>Lr |           |           |           |

***graphene, silicene, germanene, stanene,  
phosphorene, arsenene, antimonene,  
borophene...***

# X-enes group XIV: silicene, germanene, stanene

Si, Ge and Sn have an  $sp^2$ - $sp^3$  hybridization, which leads to a buckled structure.



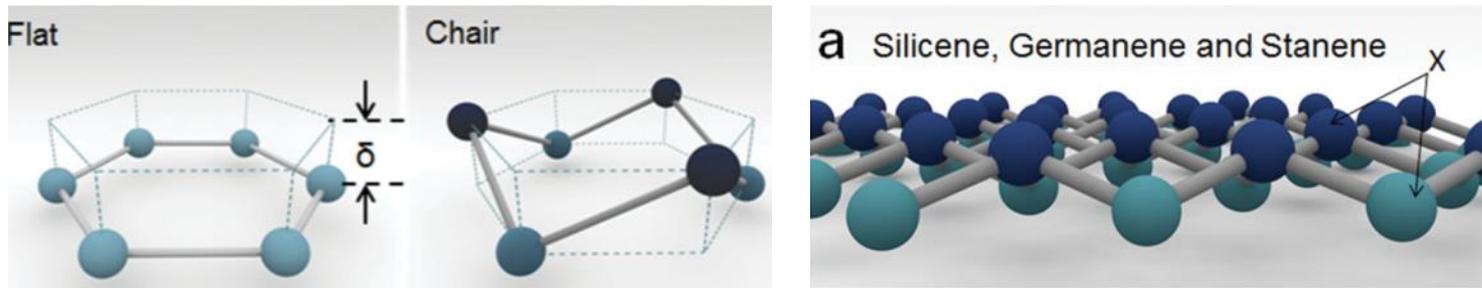
|   | C      | Si     | Ge     | Sn     |
|---|--------|--------|--------|--------|
| Lattice constant $a$ (nm)                                   | 0.2468 | 0.3868 | 0.4060 | 0.4673 |
| Bond length $d$ (nm)  | 0.1425 | 0.2233 | 0.2344 | 0.2698 |
| Buckling parameter $\delta$ (nm)                            | 0      | 0.045  | 0.069  | 0.085  |
| Effective electron mass $m^*$ ( $m_0$ )                     | 0      | 0.001  | 0.007  | 0.029  |
| Fermi velocity of carriers $V_F$ ( $10^6 \text{ ms}^{-1}$ ) | 1.01   | 0.65   | 0.62   | 0.55   |
| Energy gap $E_g$ (meV)                                      | 0.02   | 1.9    | 33     | 101    |

[Balendhran et al., Small 11, 640 (2015)]  
 [Matthes et al., J. P.hys. Cond. Mat. 25 , 395305 (2013)]

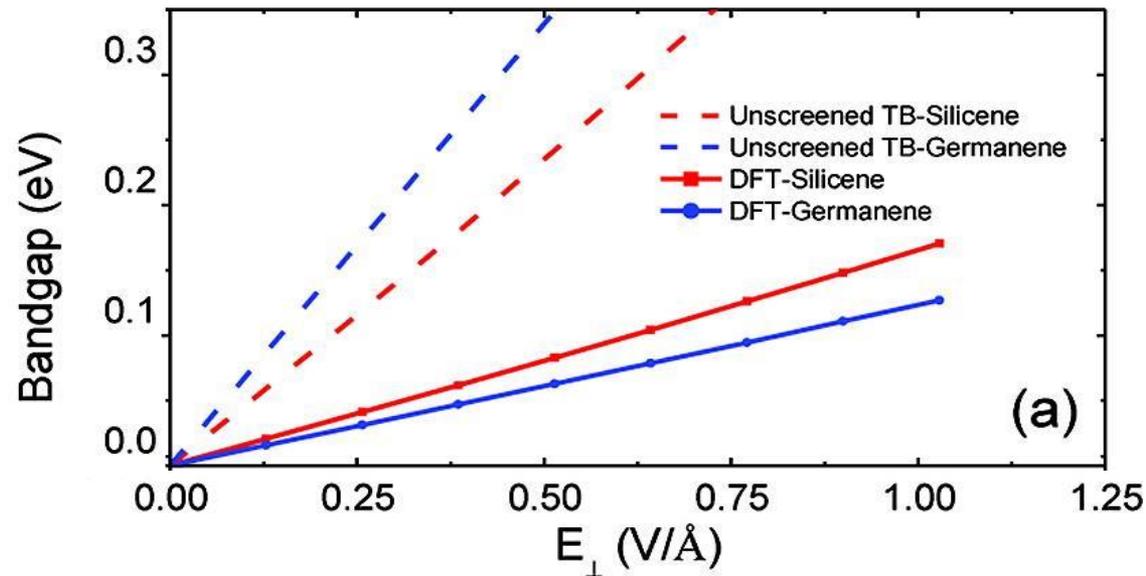
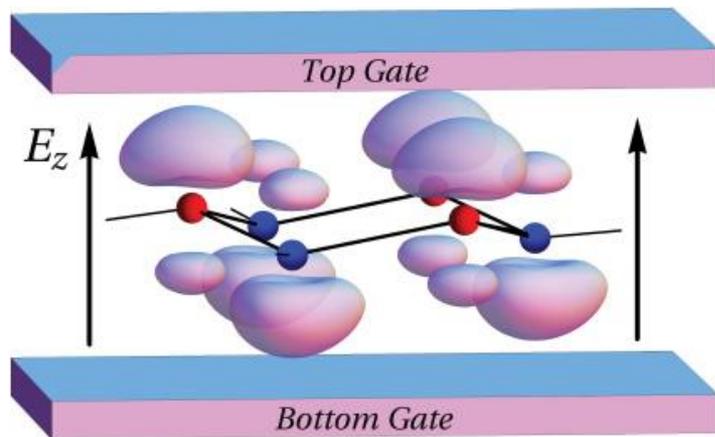


# X-enes group XIV: silicene, germanene, stanene

Si, Ge and Sn have an  $sp^2$ - $sp^3$  hybridization, which leads to a buckled structure.



A vertical electric field creates a staggered potential on A/B sublattice and generates a mass term in the Dirac equation!

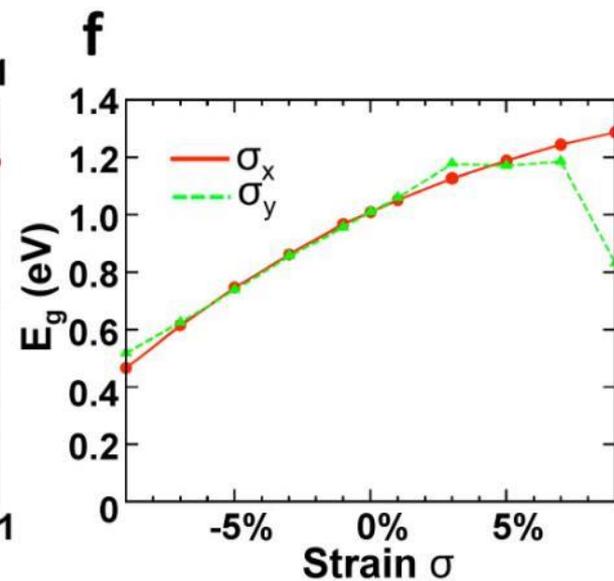
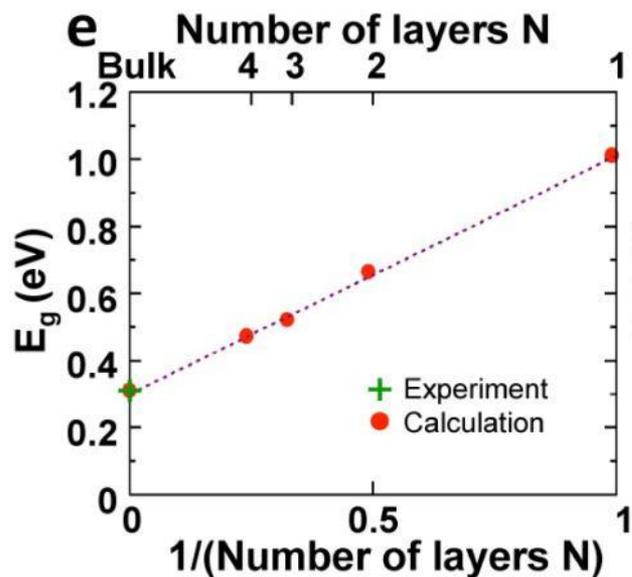
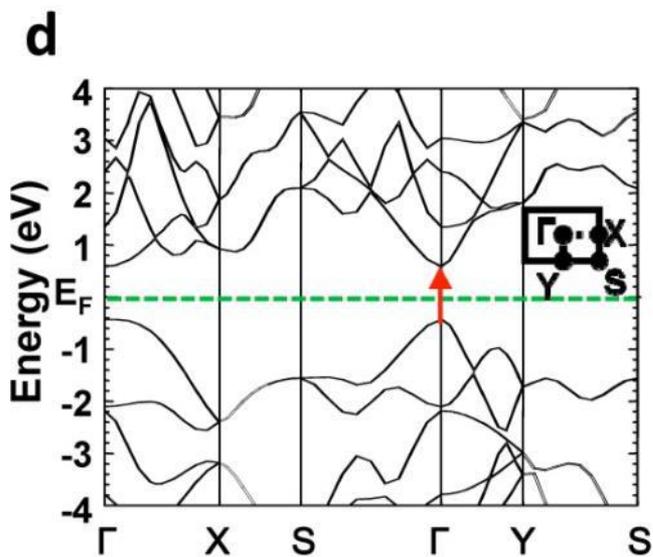
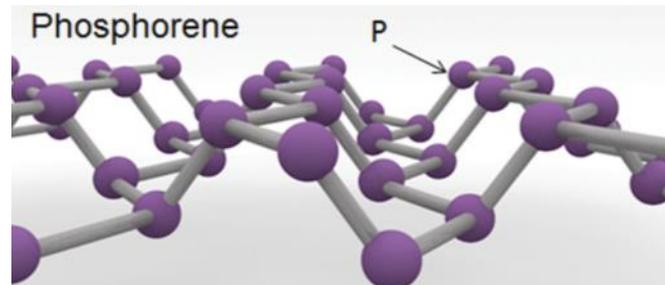
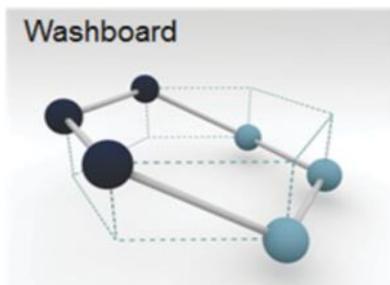


 [N. D. Drummond et al., Phys. Rev. B 85, 075423 (2012)]

 [Z. Ni et al., Nano Lett. 12,113 (2012)]

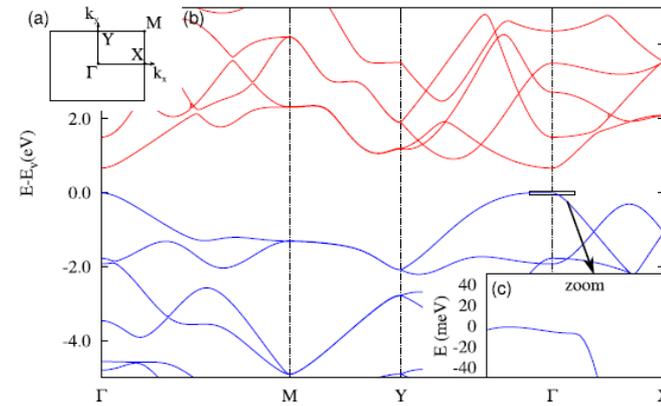
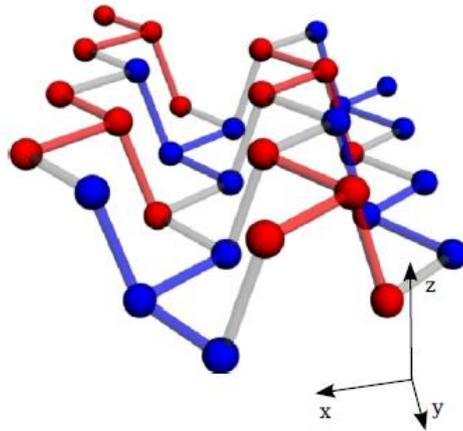
# X-enes group XIV: phosphorene, arsenene, antimonene

Its structure is puckered and it is a semiconductor!



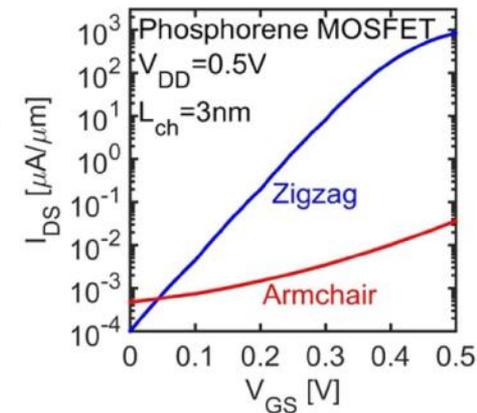
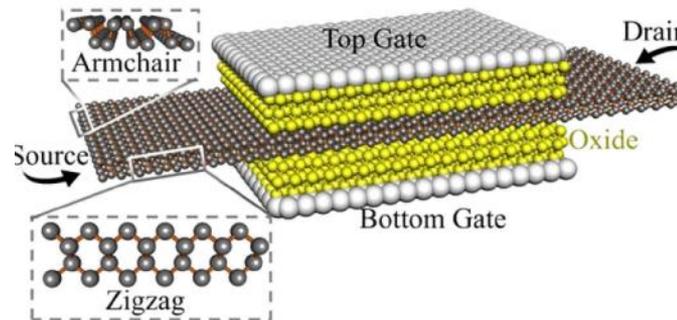
[Balendhran et al., Small 11, 640 (2015)] [H. Liu et al., ACS Nano, 8, 4033 (2014)]

# X-enes group XIV: spatial anisotropy in phosphorene



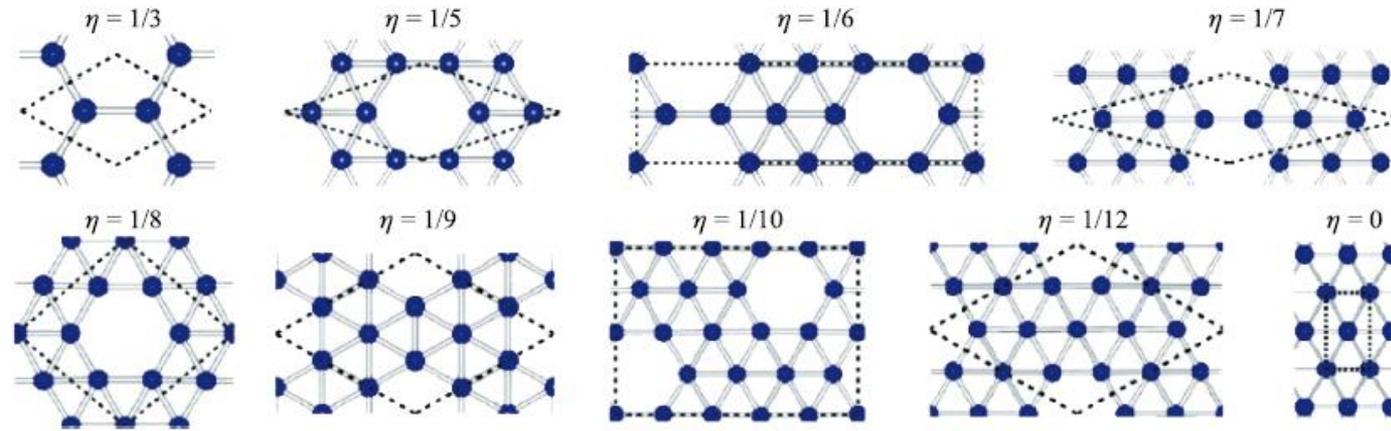
[A. S. Rodin, A. Carvalho, and A. H. Castro Neto., Phys. Rev. Lett. 112, 176801 (2014)]

| $m_{e,arm}^*$ | $m_{e,zig}^*$ | $m_{h,arm}^*$ | $m_{h,zig}^*$ | Ref.                |
|---------------|---------------|---------------|---------------|---------------------|
| 0.17          | 1.09          | 0.15          | 5.84          | TB                  |
| 0.17          | 1.12          | 0.15          | 6.35          | HSE06 <sup>26</sup> |
| 0.14          | 1.23          | 0.13          | 13.09         | PBE <sup>27</sup>   |

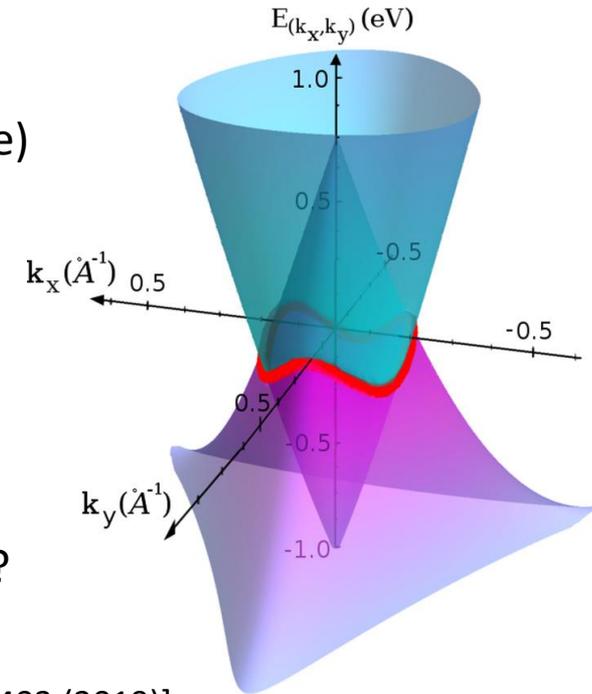


[H. Ilatikhameneh, T. Ameen, B. Novakovic, Y. Tan, G. Klimeck, R. Rahman, *Saving Moore's Law Down To 1 nm Channels With Anisotropic Effective Mass*, Scientific Reports 6, 31501 (2016)]

# X-enes group XIII: borophene



- Polymorph material: different phases with different properties
- Large and anisotropic Young's modulus (up to 1.5X graphene)
- Stretchable up to 10-15%
- Large conductivity
- Presence of Dirac cones...
- Transfer from metallic substrate
- Instable due to boron electron deficiency
- Capping as for phosphorene? Hydrogenation? Fluorination?



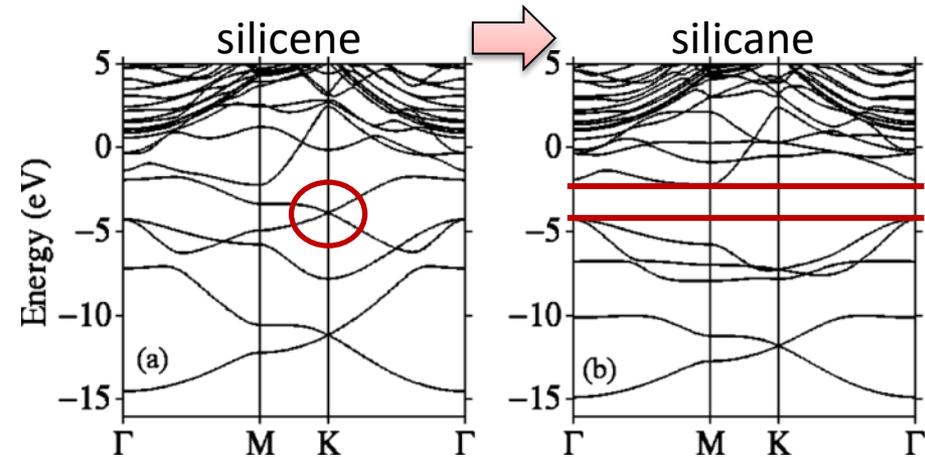
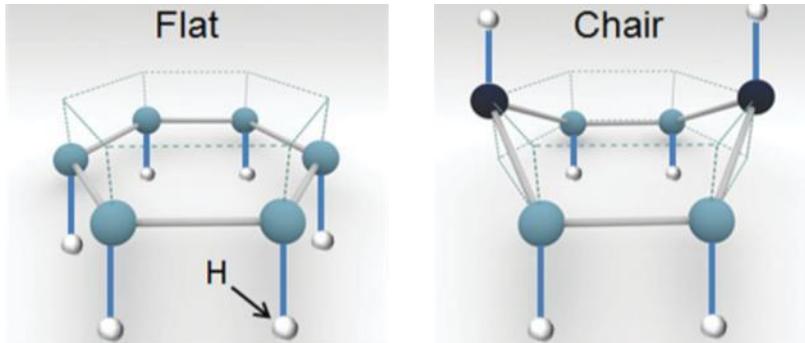
[M. Nakhaee et al., PRB98, 115413 (2018)]



[Zhi-Qiang Wang et al., Front. Phys. 14, 33403 (2019)]

# X-anes: hydrogenated X-enes

X-anes decorated with H covalently bonded to each atom of the layer



**A gap opens due to covalent bonding and the Dirac cones disappear!**

| no spin-orbit coupling is considered here                   | CH   | SiH  | GeH  |
|---|--|--|--|
| Lattice constant $a$ (nm)                                   | 0.2514                                     | 0.3820                                     | 0.4091 <sup>[21]</sup>                     |
| Metal-metal length $d$ (nm)                                 | 0.1520                                     | 0.2319                                     | 0.2338                                     |
| Metal-hydrogen length (nm)                                  | 0.1084                                     | 0.1502                                     | 0.1530                                     |
| Buckling parameter $\delta$ (nm)                            | 0.045                                      | 0.072                                      | 0.069                                      |
| Fermi velocity of carriers $V_F$ ( $10^6 \text{ ms}^{-1}$ ) | 0.63                                       | 0.51                                       | 0.38                                       |
| Energy gap $E_g$ (eV)                                       | 4.9 <sup>b)</sup> , 5.4 <sup>c)</sup> [27] | 2.9 <sup>b)</sup> , 4.0 <sup>c)</sup> [28] | 2.9 <sup>b)</sup> , 3.6 <sup>c)</sup> [28] |



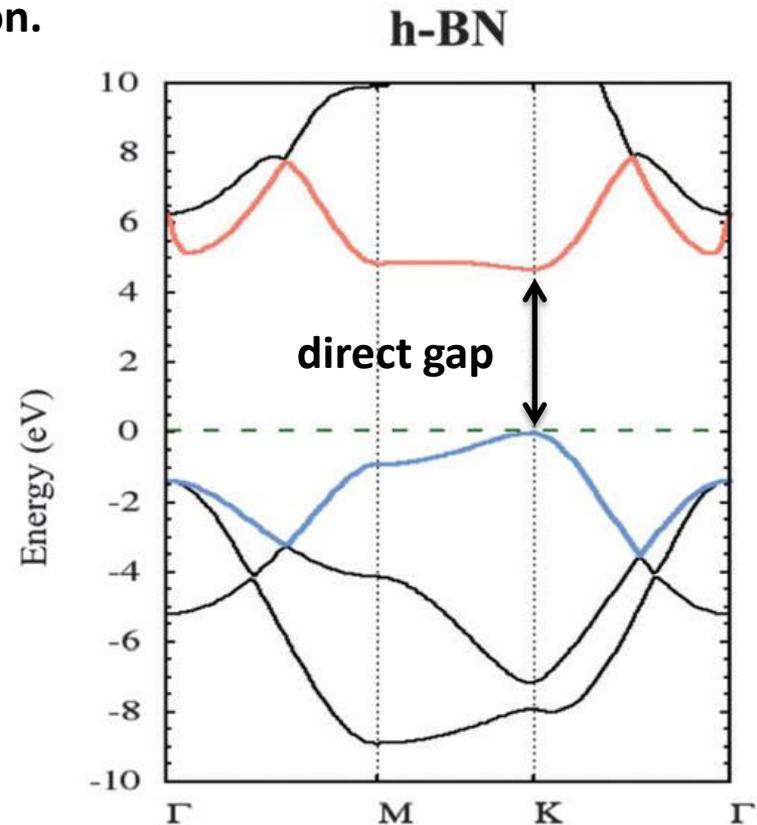
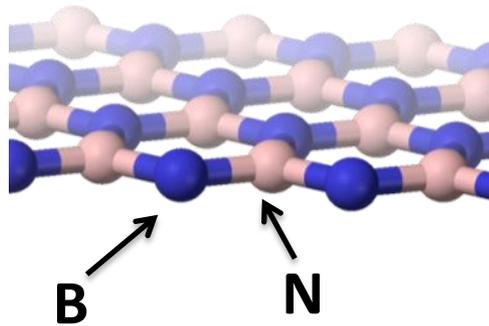
[Balendhran et al., Small 11, 640 (2015)] [H. Liu et al., ACS Nano, 8, 4033 (2014)]  
 [L. C. Lew Yan Voon et al, Appl. Phys. Lett. 97, 163114 (2010)]

# h-BN: hexagonal boron nitride

Isoelectronic analog of graphene with  $sp^2$  hybridization.

13 14 15 16 17 18

|           |           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|
|           |           |           |           |           | 2<br>He   |
| 5<br>B    | 6<br>C    | 7<br>N    | 8<br>O    | 9<br>F    | 10<br>Ne  |
| 13<br>Al  | 14<br>Si  | 15<br>P   | 16<br>S   | 17<br>Cl  | 18<br>Ar  |
| 31<br>Ga  | 32<br>Ge  | 33<br>As  | 34<br>Se  | 35<br>Br  | 36<br>Kr  |
| 49<br>In  | 50<br>Sn  | 51<br>Sb  | 52<br>Te  | 53<br>I   | 54<br>Xe  |
| 81<br>Tl  | 82<br>Pb  | 83<br>Bi  | 84<br>Po  | 85<br>At  | 86<br>Rn  |
| 113<br>Nh | 114<br>Fl | 115<br>Mc | 116<br>Lv | 117<br>Ts | 118<br>Og |



- Due to the different electronegativity of B and N, the two sublattices are no more equivalent and a gap opens!
- The lattice parameter is very similar to that of graphene: excellent substrate



[P. Miró, M. Audiffred and T. Heine, *An atlas of two-dimensional materials*, Chem. Soc. Rev. 43, 6537 (2014)]

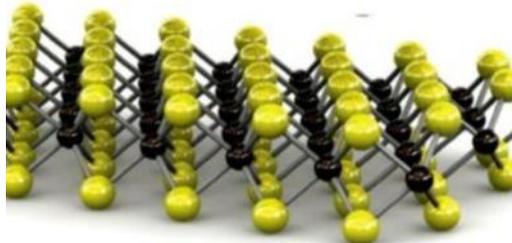
# Transition metal dichalcogenides (TMDs)

$\text{MX}_2$  where M is a transition metal (partially filled d sub-shell) and X a chalcogen (S, Se, Te).

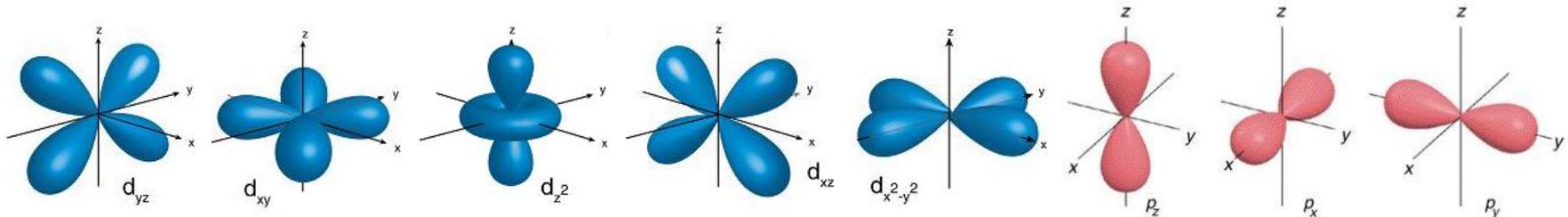
Group → 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18

↓ Period

|         |          |          |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |
|---------|----------|----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 1       | 2        |          |           |           |           |           |           |           |           |           |           | 18        |           |           |           |           |           |
| 1<br>H  |          |          |           |           |           |           |           |           |           |           |           |           |           |           |           |           | 2<br>He   |
| 2<br>Li | 4<br>Be  |          |           |           |           |           |           |           |           |           |           | 5<br>B    | 6<br>C    | 7<br>N    | 8<br>O    | 9<br>F    | 10<br>Ne  |
| 3<br>Na | 12<br>Mg |          |           |           |           |           |           |           |           |           |           | 13<br>Al  | 14<br>Si  | 15<br>P   | 16<br>S   | 17<br>Cl  | 18<br>Ar  |
| 4<br>K  | 20<br>Ca | 21<br>Sc | 22<br>Ti  | 23<br>V   | 24<br>Cr  | 25<br>Mn  | 26<br>Fe  | 27<br>Co  | 28<br>Ni  | 29<br>Cu  | 30<br>Zn  | 31<br>Ga  | 32<br>Ge  | 33<br>As  | 34<br>Se  | 35<br>Br  | 36<br>Kr  |
| 5<br>Rb | 38<br>Sr | 39<br>Y  | 40<br>Zr  | 41<br>Nb  | 42<br>Mo  | 43<br>Tc  | 44<br>Ru  | 45<br>Rh  | 46<br>Pd  | 47<br>Ag  | 48<br>Cd  | 49<br>In  | 50<br>Sn  | 51<br>Sb  | 52<br>Te  | 53<br>I   | 54<br>Xe  |
| 6<br>Cs | 56<br>Ba |          | 72<br>Hf  | 73<br>Ta  | 74<br>W   | 75<br>Re  | 76<br>Os  | 77<br>Ir  | 78<br>Pt  | 79<br>Au  | 80<br>Hg  | 81<br>Tl  | 82<br>Pb  | 83<br>Bi  | 84<br>Po  | 85<br>At  | 86<br>Rn  |
| 7<br>Fr | 88<br>Ra |          | 104<br>Rf | 105<br>Db | 106<br>Sg | 107<br>Bh | 108<br>Hs | 109<br>Mt | 110<br>Ds | 111<br>Rg | 112<br>Cn | 113<br>Nh | 114<br>Fl | 115<br>Mc | 116<br>Lv | 117<br>Ts | 118<br>Og |



|             |          |          |          |          |          |          |          |          |          |          |          |           |           |           |           |
|-------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|-----------|-----------|-----------|
| Lanthanides | 57<br>La | 58<br>Ce | 59<br>Pr | 60<br>Nd | 61<br>Pm | 62<br>Sm | 63<br>Eu | 64<br>Gd | 65<br>Tb | 66<br>Dy | 67<br>Ho | 68<br>Er  | 69<br>Tm  | 70<br>Yb  | 71<br>Lu  |
| Actinides   | 89<br>Ac | 90<br>Th | 91<br>Pa | 92<br>U  | 93<br>Np | 94<br>Pu | 95<br>Am | 96<br>Cm | 97<br>Bk | 98<br>Cf | 99<br>Es | 100<br>Fm | 101<br>Md | 102<br>No | 103<br>Lr |

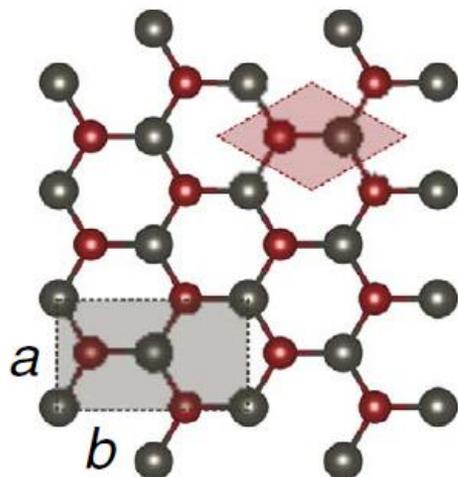
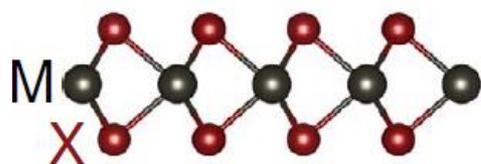


[F. A. Rasmussen and K. S. Thygesen, *Computational 2D Materials Database: Electronic Structure of Transition-Metal Dichalcogenides and Oxides*, J. Phys. Chem. C 119, 13169 (2015)]

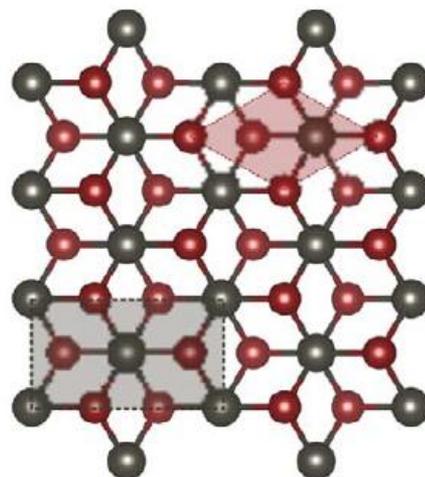
[S. Manzeli et al., 2D transition metal dichalcogenides, *Nature Reviews Materials* 2, 17033 (2017)]



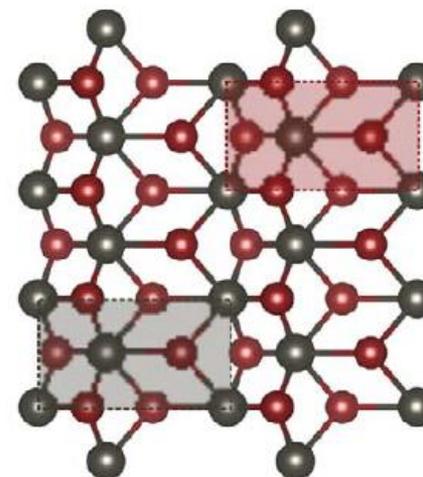
# Transition metal dichalcogenides: 2H, 1T and 1T' phases



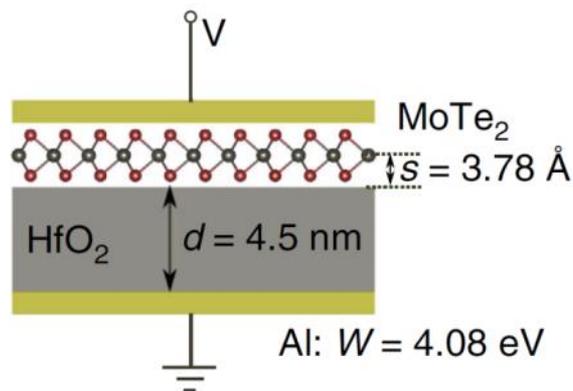
2H : trigonal prismatic



1T : distorted octahedral



1T' : dimerized 1T



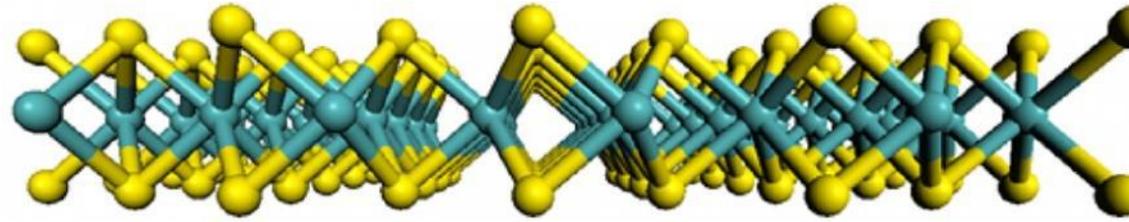
In some materials, the phase is predicted to be **switchable** by an electric field!



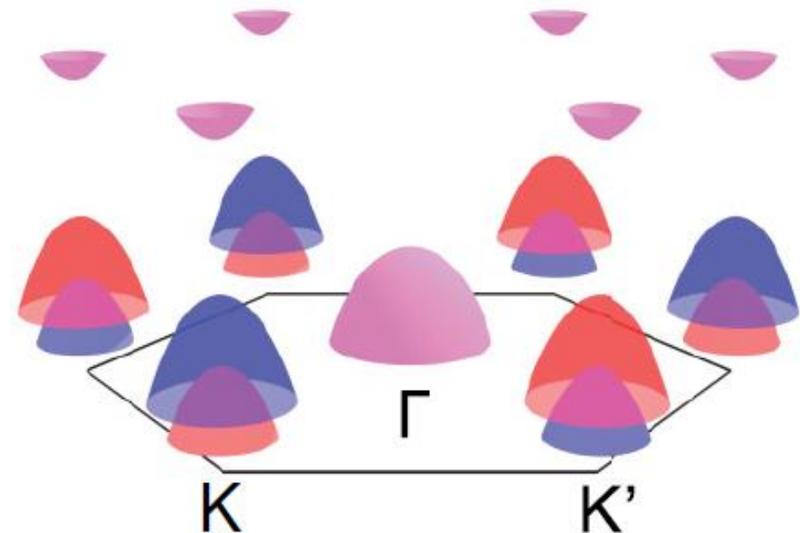
[Y. Li et al., Nat. Comm. 7, 10671 (2016)]

# Transition metal dichalcogenides: group VI

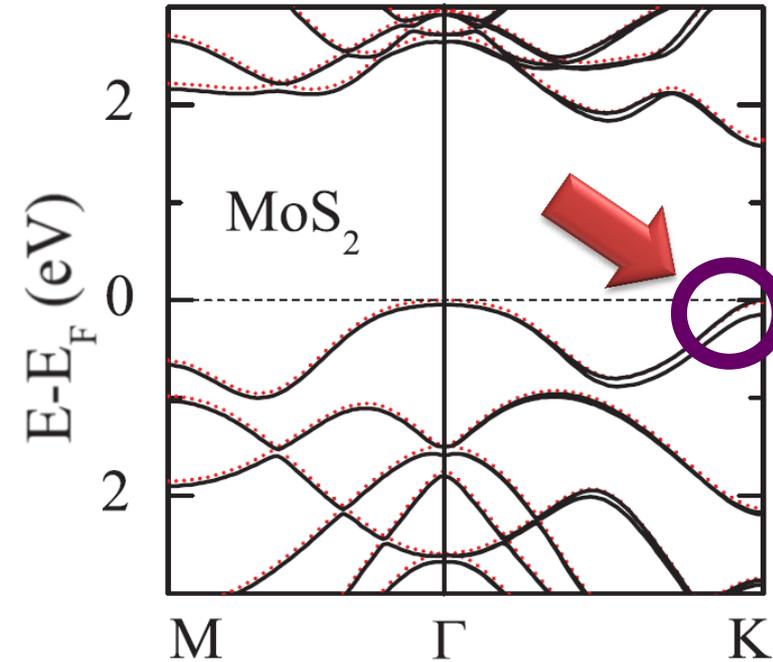
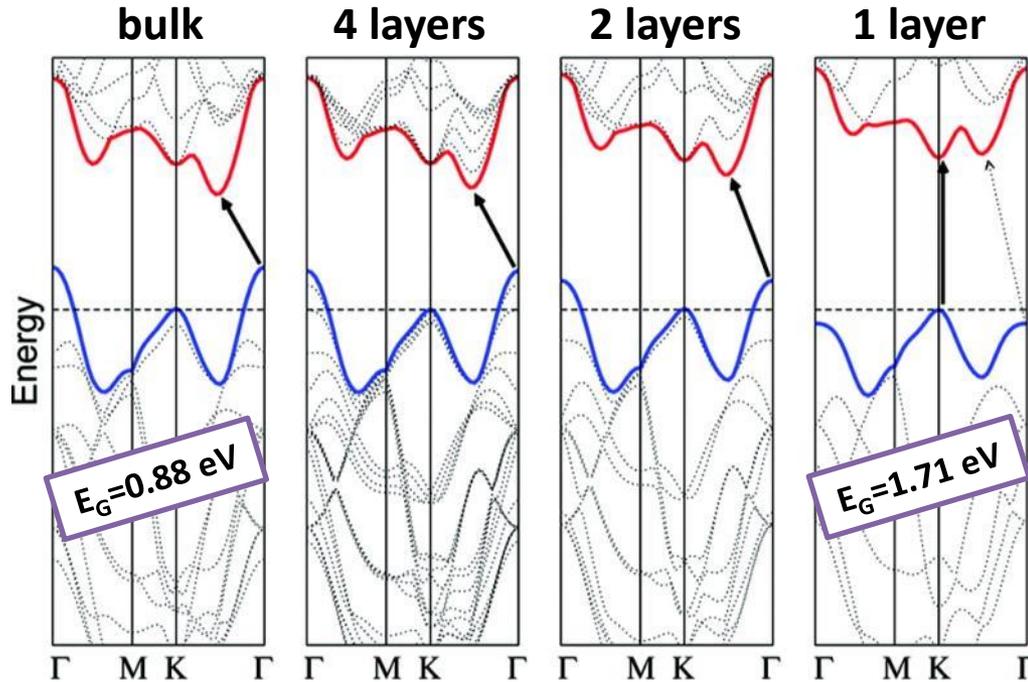
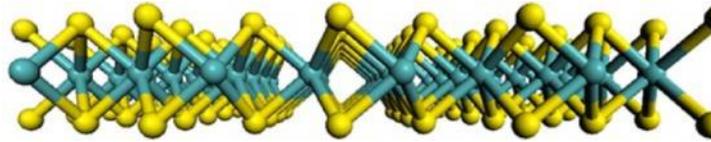
2H phase, semiconductor  
 $\text{MoS}_2$  /  $\text{MoSe}_2$  /  $\text{WS}_2$  /  $\text{WSe}_2$



- Conduction band minima and valence band maxima at **K and K'** points of the Brillouin zone: **direct gap**
- **Strong spin-orbit** coupling due to heavy atoms
- Lack of inversion symmetry in the 2H phase: **strong spin-splitting at K/K'** points (inversion symmetry recovered for bilayer!)
- ✓ Time reversal symmetry  $E^\uparrow(\mathbf{k})=E^\downarrow(-\mathbf{k})$
- ✗ Spatial inversion symmetry  $E^\uparrow(\mathbf{k})=E^\uparrow(-\mathbf{k})$
- ✗  $\rightarrow E^\uparrow(\mathbf{k})=E^\downarrow(\mathbf{k})$  *Kramer's degeneracy*
- **Spin-valley coupling:**  
valley polarization = spin polarization



# MoS<sub>2</sub> molybdenum disulfide (TMDs - group VI)

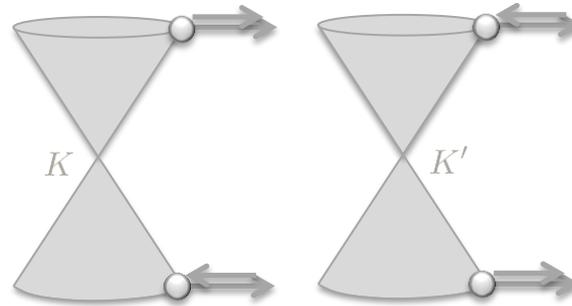
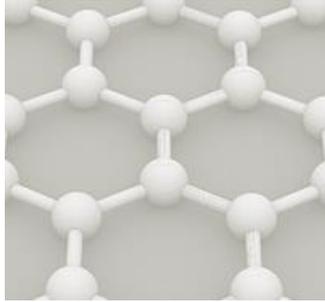


[Z. Y. Zhu et al., PRB 84, 153402 (2011)]

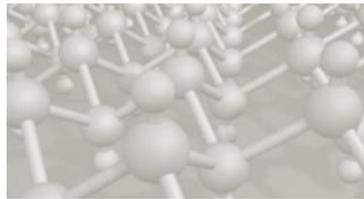
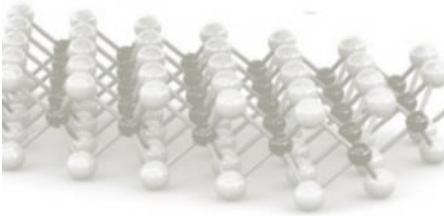
- The gap increases when decreasing the layer number and becomes direct
- The spin-orbit splitting of the valence band is **~150meV**

# Plan

- Graphene: structure and properties



- Other 2D materials: TMDs, SMCs, X-enes, X-anes...



- Applications of 2D materials: electronics, optoelectronics, spintronics and many more



# Electronics: field effect transistors

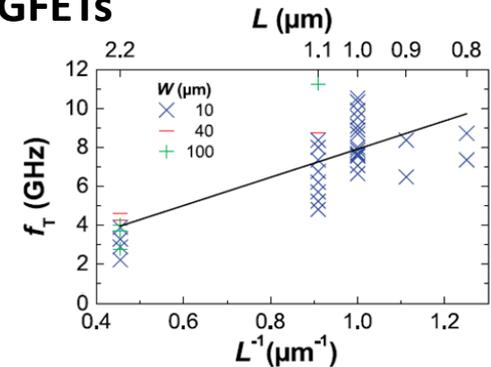
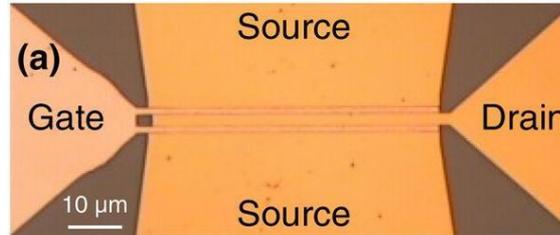
## Graphene



- ✓ high charge mobility
- ✓ excellent electrostatic control
- ✗ no gap

[E. Guerriero et al., *Scient. Rep.* 7, 2419 (2017)]

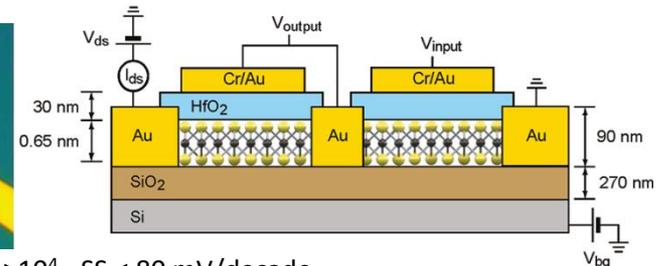
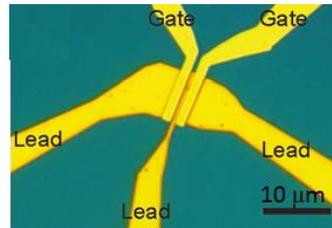
## high-frequency analog GFETs



## Transition metal dichalcogenides

- ✓ excellent electrostatic control
- ✓ do have a gap
- ✓ self-passivated surface
- ✓ van der Waals heterostructures
- ✗ low mobility (not a problem for ultrascaled channel lengths)

## Field effect transistors/integrated circuits for logic operations



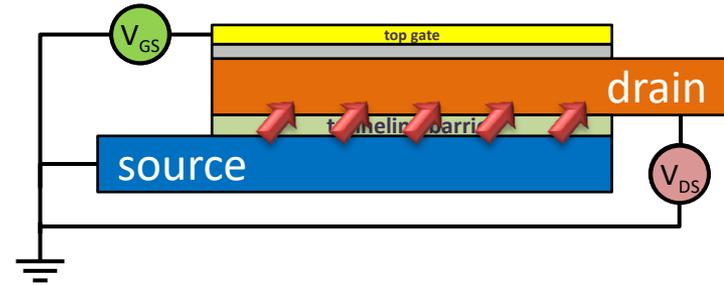
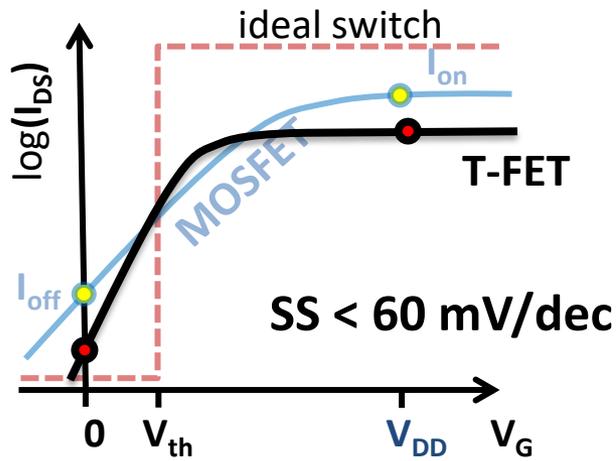
$$I_{on}/I_{off} > 10^4 - SS < 80 \text{ mV/decade}$$

[B. Radisavljevic et al., *ACS Nano* 5, 9934 (2011)]

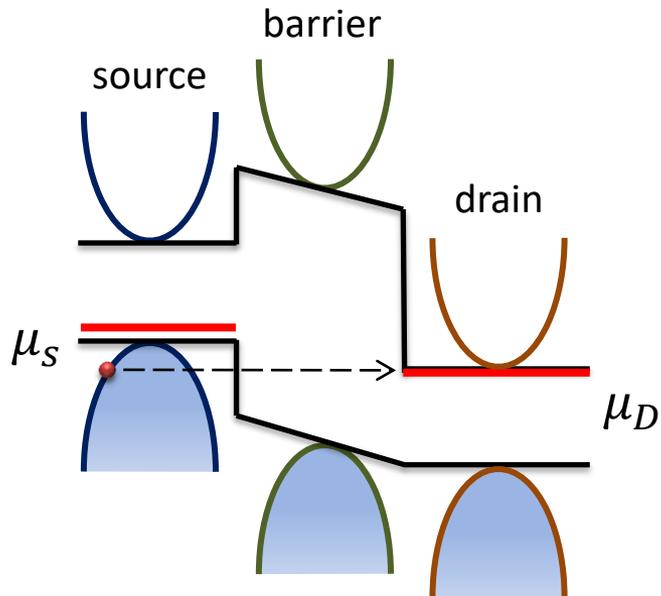
## However

- ✗ not competitive with Si technology for high performance computing
- ✗ Ohmic contacts difficult to obtain

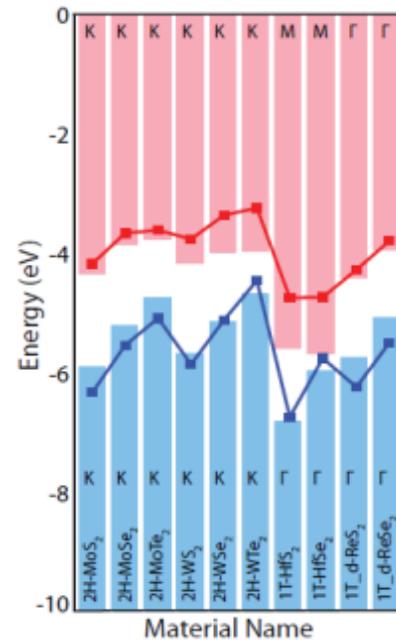
# Electronics: low power tunnel field effect transistors



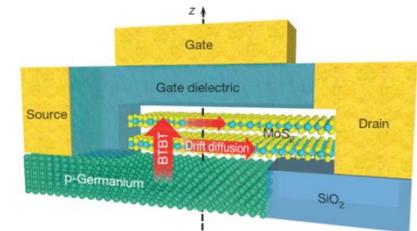
staggered band alignment



vdW heterostructures

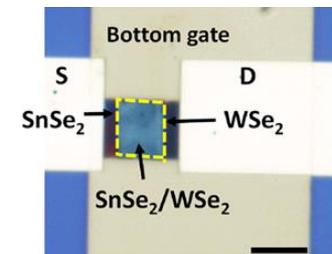


Ge/MoS<sub>2</sub> TFET



[D. Sarkar et al., Nature **526**, 91 (2015)]

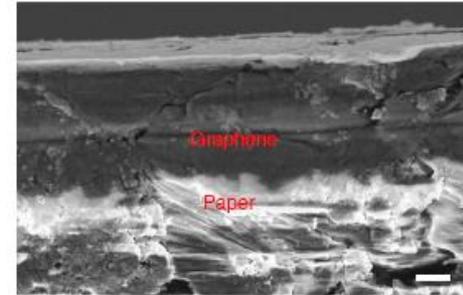
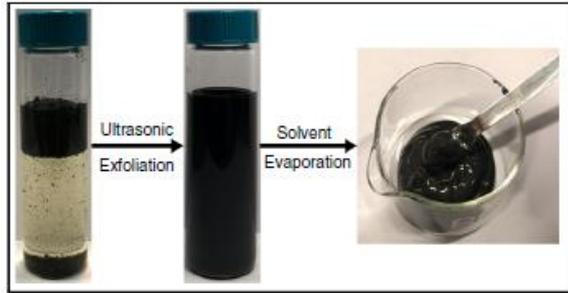
SnSe<sub>2</sub>/WSe<sub>2</sub> vdW TFET



[T. Roy et al., APL **108**, 083111 (2016)]

# Printable, low-cost and flexible electronics

## Graphene as low-cost printable conductive ink



Conductivity up to  $7.13 \times 10^4 \text{ S m}^{-1}$ , (silver  $10^6 \text{ S m}^{-1}$ )

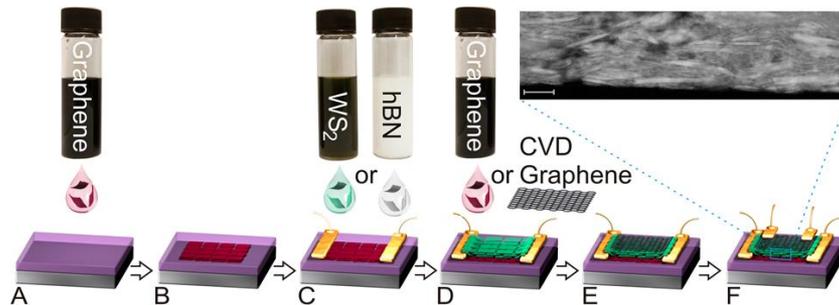
[K. Pan et al., Nat. Comm. 9, 5197 (2018)]



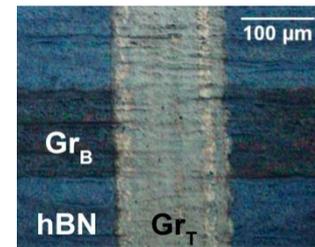
Graphene ink : RFIDs, antenna, wearables...



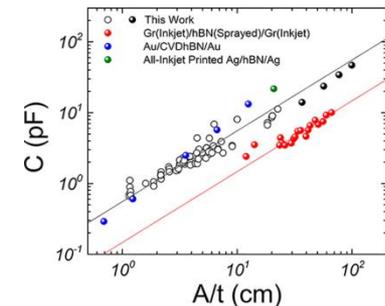
## Ink and ink-jet printing of 2D heterostructures



[F. Withers et al., Nano Lett. 14, 3987 (2014)]



capacitor



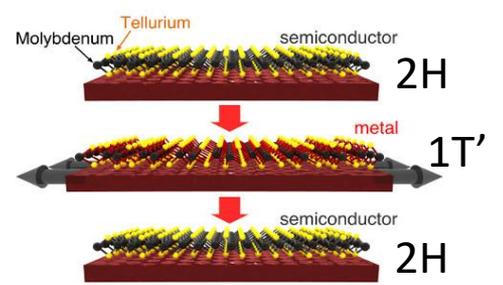
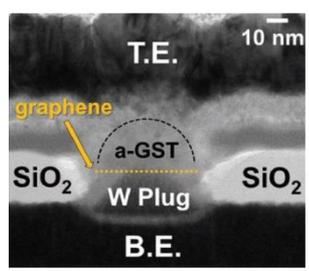
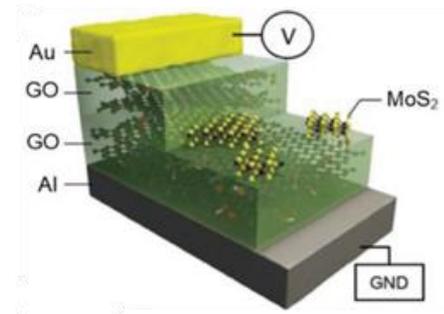
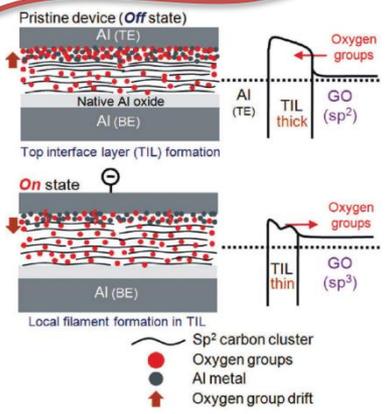
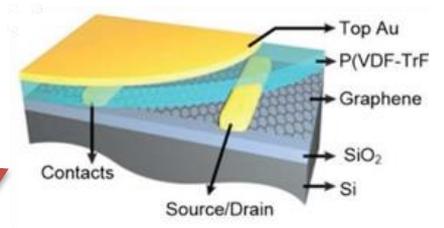
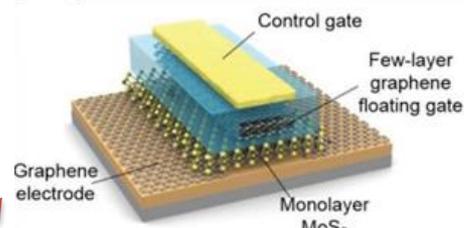
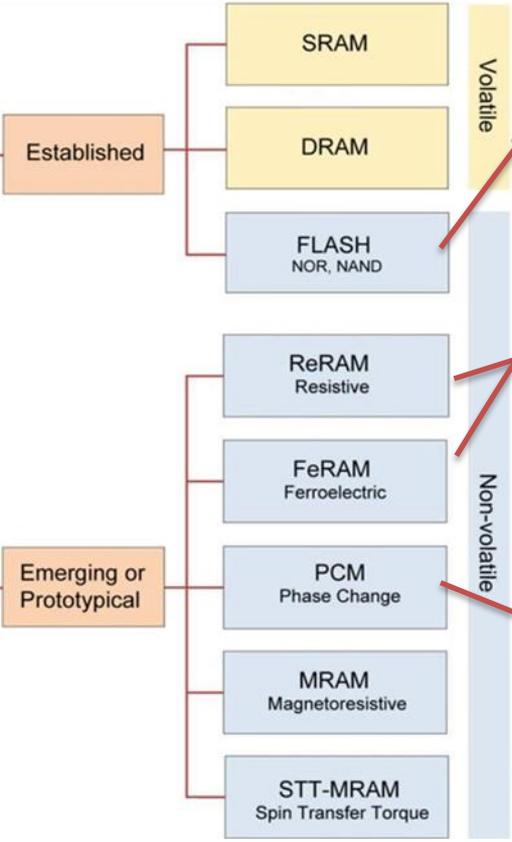
[R. Worsley et al., ACS Nano 13, 54 (2019)]

# Electronics: non-volatile memories

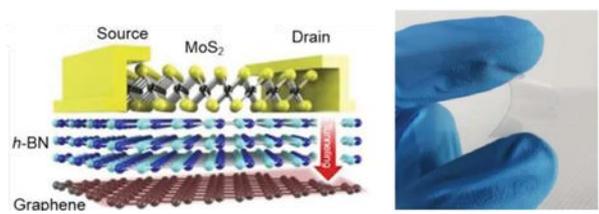


[S. Bertolazzi et al., Adv. Mater. 31, 1806663 (2019)]

Memory Technologies



[K.-A. N. Duerloo et al., Nat. Comm. 5, 4214 (2014)]



[Q. A. Vu et al., Nat. Comm. 7, 12725 (2016)]

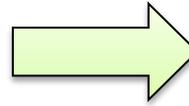


[R. Wang et al., Adv. Funct. Mater. 28, 1802473 (2018)]

Charge doping  
Strain  
Thermal treatment

# Spintronics

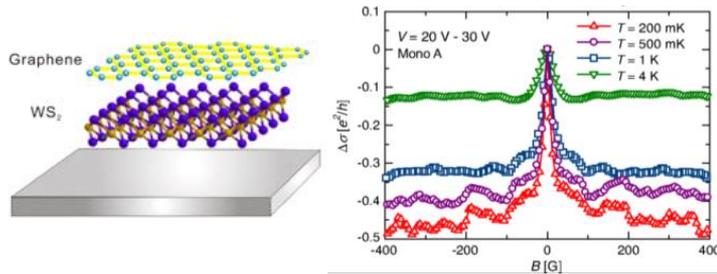
Spin length  $> 10 \mu\text{m}$  @room temperature  
for graphene over hBN



all-graphene-based spintronics

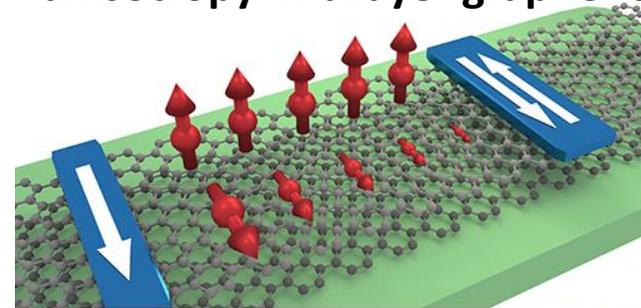
## How to manipulate spin?

Proximity effect: inducing spin-orbit coupling  
in graphene on TMDs



[T. Wakamura et al., Phys. Rev. Lett. 120, 106802 (2018)]

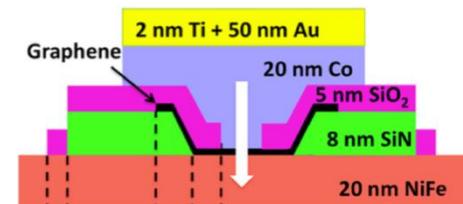
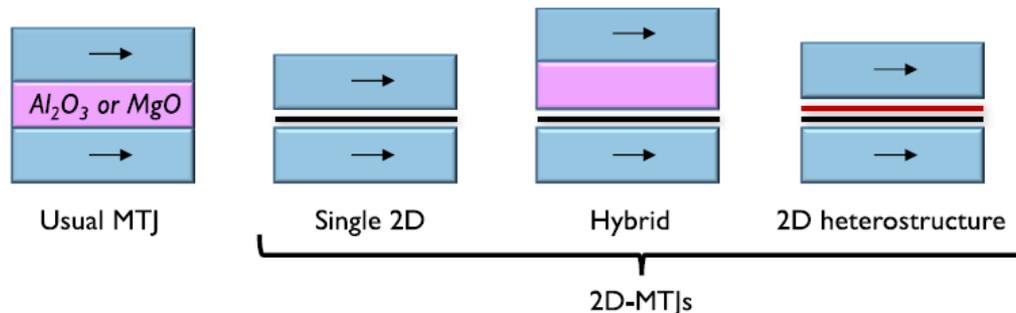
Electric-field induced spin relaxation  
anisotropy in bilayer graphene



T. Ghiasi/University of Groningen

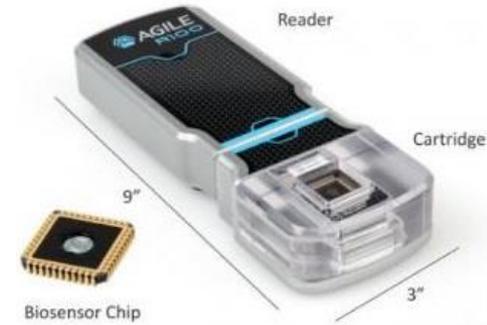
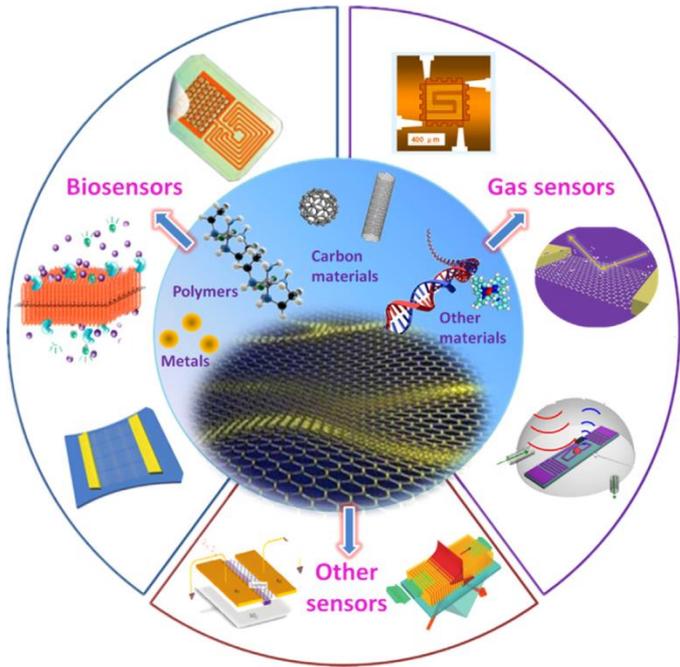
[J. C. Leutenantsmeyer, PRL 121, 127702 (2018)]

## Magnetic tunnel junction for giant magnetoresistance

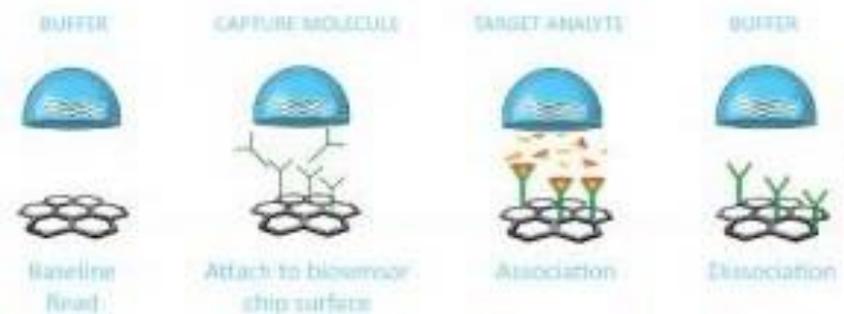


[M. Piquemal-Banci et al., J. Phys. D: Appl. Phys. 50, 203002 (2017)]

# Graphene for sensing and health



## AGILE R100 WORKFLOW

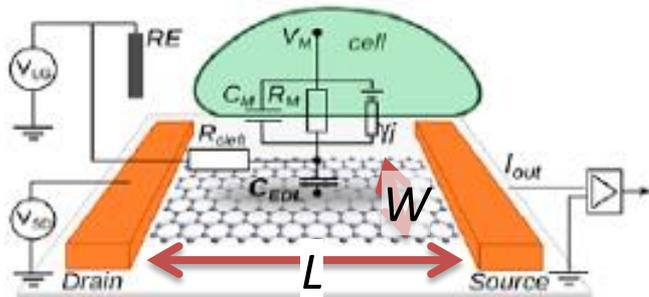


[X. Yu et al., Biosens. and Bioelec. 89, 77 (2017)]

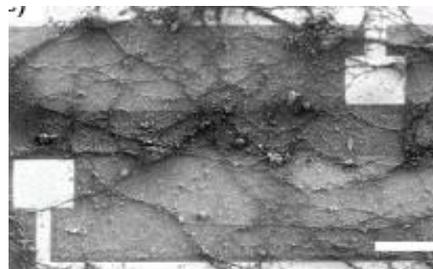
[C. Anichini et al., Chem. Soc. Rev. 47, 4860 (2018)]

## *In vivo* sensing of neuron ion channel activity

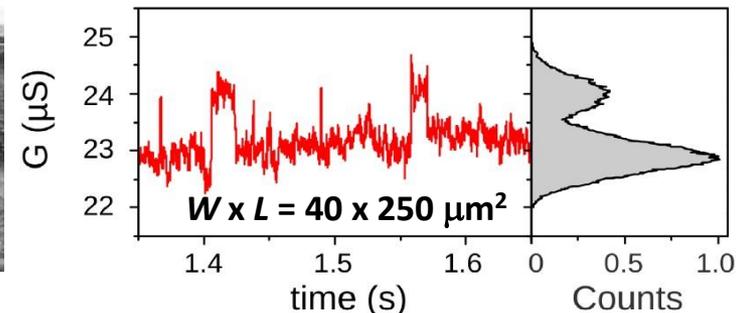
[F. Veliev et al., 2D Materials 5, 045020 (2018)]



## neuron network



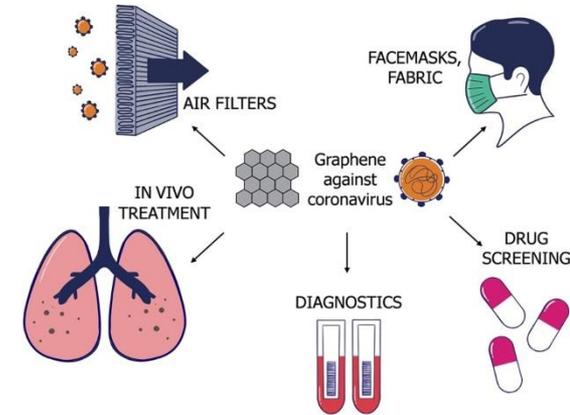
## conductance vs time



## Can graphene take part in the fight against COVID-19?

V. Palmieri and M.Papi **nanotoday** *in press*

<https://doi.org/10.1016/j.nantod.2020.100883>



- Functionalized graphene can **capture viruses** and **deliver antiviral drugs**.
- Viruses on graphene can be inactivated by light or heat treatments.
- Graphene can be used as **coating material** for medical devices, personal protective equipment or facemasks to minimize the risk of transmission.
- Graphene-based **sensors** can be embedded in textiles and environmental filters or used for high-throughput screening of virus helicase inhibitors.

[www.acsnano.org](http://www.acsnano.org)

## Reusable and Recyclable Graphene Masks with Outstanding Superhydrophobic and Photothermal Performances

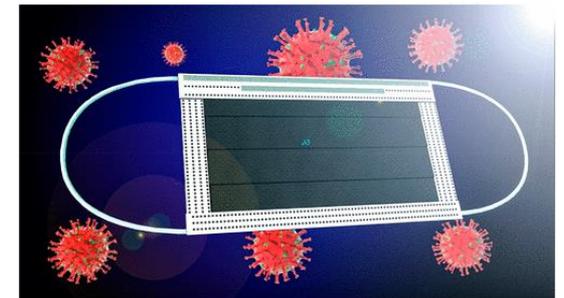
Hong Zhong, Zhaoran Zhu, Jing Lin, Chi Fai Cheung, Vivien L. Lu, Feng Yan, Ching-Yuen Chan, and Guijun Li\*



Cite This: <https://dx.doi.org/10.1021/acsnano.0c02250>



Read Online



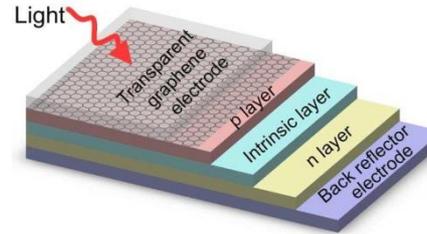
# Optoelectronics

## Graphene as an electrode

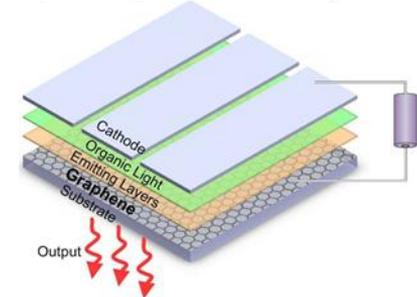
- transparent
- highly conductive
- flexible

[F. Bonaccorso et al., Nat. Phot. 4, 611 (2010)]

## silicon solar cell

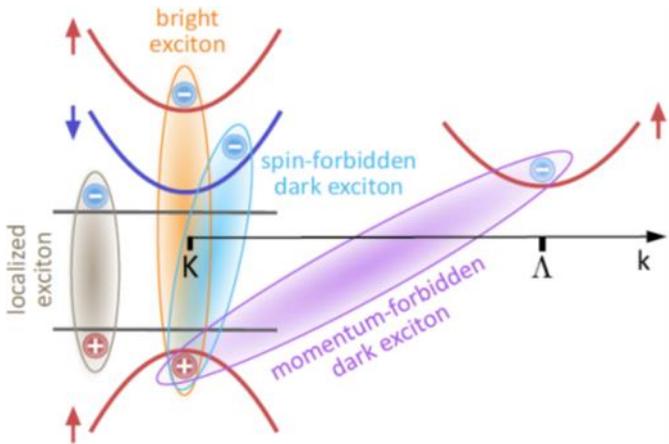


## organic LED



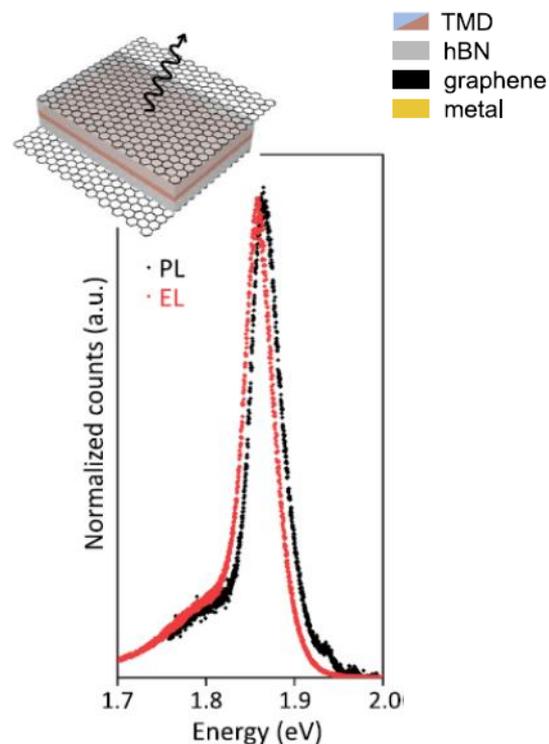
## Excitons in transition metal dichalcogenides

- room temperature (binding energy  $\sim 0.5\text{eV}$ )
- reach SOC and multivalley physics
- interlayer excitons in vdW heterostructures

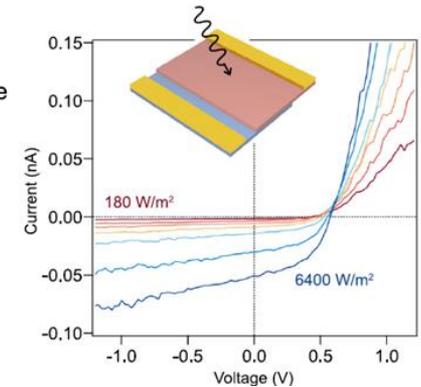


[T. Mueller et al., npj 2D Materials and Applications 2, 29 (2018)]

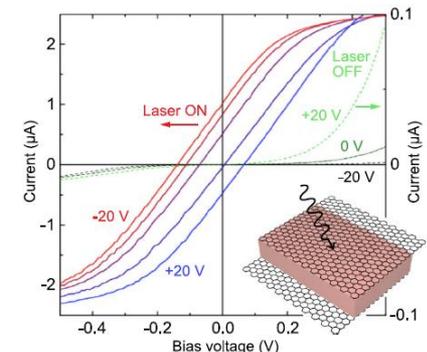
## excitonic light emission



## photovoltaic solar cells



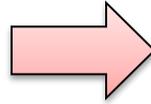
## photodetectors



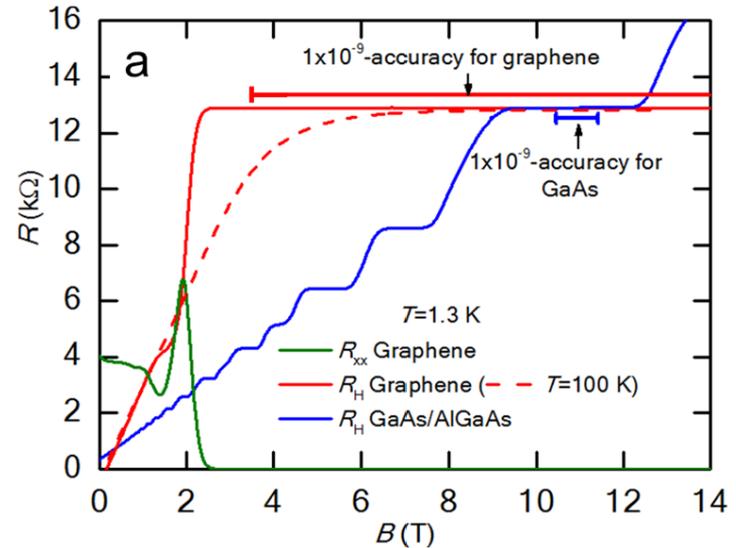
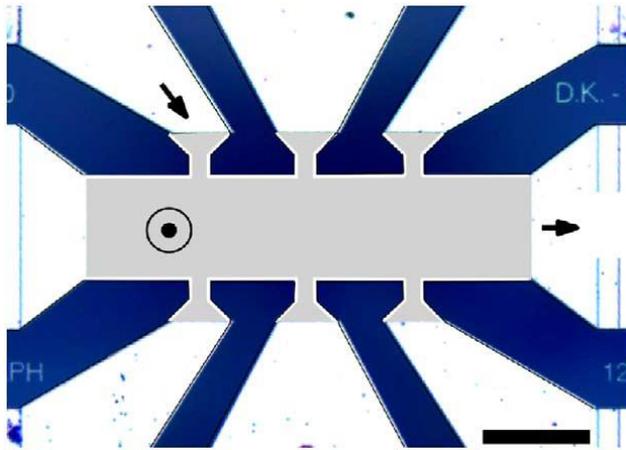
# Metrology: graphene as a resistance standard

## Energy spacing Landau levels

- GaAs-based Hall bars  $\Delta E \approx 1.7B[\text{T}]\text{meV}$
- graphene-based  $\Delta E \approx 35\sqrt{B[\text{T}]}\text{meV}$



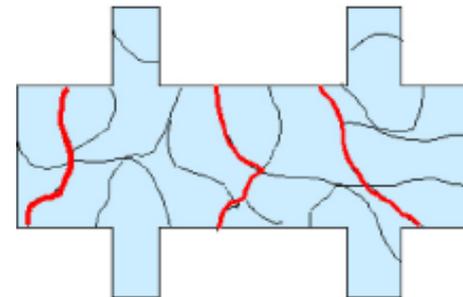
- low magnetic fields ( $B < 4\text{ T}$ )
- higher temperature ( $T > 4\text{ K}$ )
- higher measurement current ( $I > 100\ \mu\text{A}$ )



[F. Lafont et al, Nat. Commun. 6, 6806 (2015)]

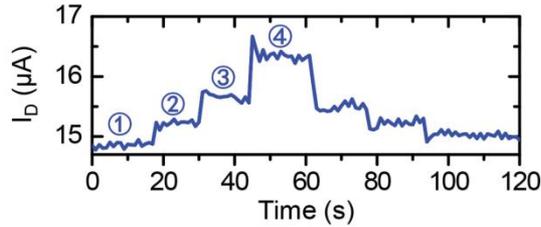
**Importance of graphene quality:** grain boundaries in CVD graphene can create a network of conductive paths

[A. Cumming et al., PRB 90, 161401 (2014)]



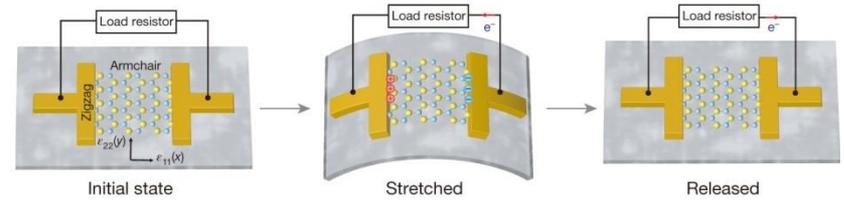
# Mechanics

## Strain Sensors

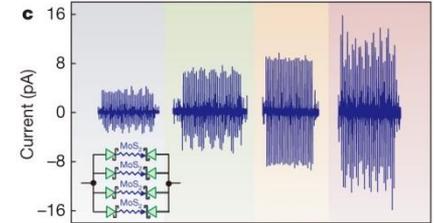


[Q. Sun et al., Adv. Mat. 27, 3411 (2015)]

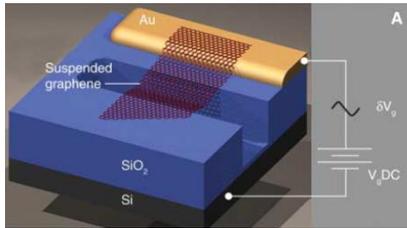
## Piezoelectric generators



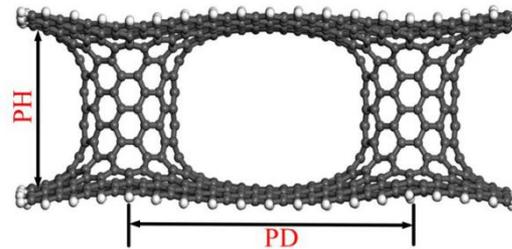
[W. Wu et al., Nature 514, 470 (2014)]



## Resonators and mass detection



[J. S. Bunch et al., Science 315, 490 (2007)]



[K. Duan et al., Scient. Report. 7, 14012 (2017)]

Sensitivity 1 yg ( $10^{-24}$  g)  
Mass responsivity 0.34 GHz/yg

## Mechanical reinforcement



# Conclusion

- 2D materials represent an **amazing discovery** in material science
- They attracted much interest for both **fundamental physics** and **applications**
- Many new 2D materials are to be predicted, exfoliated or synthesized
- **van der Waals coupling** allows the engineering of vertical heterostructures with specific properties
- Large **variety of applications** in different fields
- **Material quality** and **fabrication techniques** are critical issues for many applications
- ...there is still a lot to do

## Thanks for your attention!